# Package 'BGGM'

February 23, 2024

Type Package

Title Bayesian Gaussian Graphical Models

Version 2.1.1

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Description Fit Bayesian Gaussian graphical models. The methods are separated into two Bayesian approaches for inference: hypothesis testing and estimation. There are extensions for confirmatory hypothesis testing, comparing Gaussian graphical models, and node wise predictability. These methods were recently introduced in the Gaussian graphical model literature, including Williams (2019) <doi:10.31234/osf.io/x8dpr>, Williams and Mulder (2019) <doi:10.31234/osf.io/ypxd8>,

Williams, Rast, Pericchi, and Mulder (2019) <doi:10.31234/osf.io/yt386>.

## **Depends** R (>= 4.3.0)

# License GPL-2

- **Imports** BFpack (>= 1.2.3), GGally (>= 1.4.0), ggplot2 (>= 3.2.1), ggridges (>= 0.5.1), grDevices, MASS (>= 7.3-51.5), methods, mvnfast (>= 0.2.5), network (>= 1.15), reshape (>= 0.8.8), Rcpp (>= 1.0.4.6), Rdpack (>= 0.11-1), sna (>= 2.5), stats, utils,
- Suggests abind (>= 1.4-5), assortnet (>= 0.12), networktools (>= 1.3.0), mice (>= 3.8.0), psych, knitr, rmarkdown, testthat (>= 3.0.0)

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RdMacros Rdpack

BugReports https://github.com/donaldRwilliams/BGGM/issues

Config/testthat/edition 3

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# **R** topics documented:

asd_ocd	4
bfi	
bggm_missing	6
coef.estimate	8
coef.explore	9
confirm	11
constrained_posterior	14
convergence	
csws	
depression_anxiety_t1	
depression_anxiety_t2	
estimate	
explore	
fisher_r_to_z	
fisher_z_to_r	
gen_net	
gen_ordinal	
ggm_compare_confirm	
ggm_compare_estimate	
ggm_compare_explore	
ggm_compare_ppc	
gss	
ifit	
impute_data	53
iri	55
map	
pcor_mat	
pcor_sum	
pcor_to_cor	
plot.confirm	
plot.ggm_compare_ppc	
plot.pcor_sum	64
plot.predictability	65
plot.roll_your_own	
plot.select	67
plot.summary.estimate	
plot.summary.explore	
plot.summary.ggm_compare_estimate	71

plot.summary.ggm_compare_explore
plot.summary.select.explore
plot.summary.var_estimate
plot_prior
posterior_predict
posterior_samples
precision
predict.estimate
predict.explore
predict.var_estimate
predictability
predicted_probability
print.BGGM
prior_belief_ggm
prior_belief_var
ptsd
ptsd_cor1
ptsd_cor2
ptsd_cor3
ptsd_cor4
regression_summary
roll_your_own
rsa
Sachs
select
select.estimate
select.explore
select.ggm_compare_estimate
select.ggm_compare_explore
select.var_estimate
summary.coef
summary.estimate
summary.explore
summary.ggm_compare_estimate
summary.ggm_compare_explore
summary.predictability
summary.select.explore
summary.var_estimate
tas
var_estimate
weighted_adj_mat
women_math
zero_order_cors

asd\_ocd

## Description

A correlation matrix with 17 variables in total (autsim: 9; OCD: 8). The sample size was 213.

## Usage

```
data("asd_ocd")
```

## Format

A correlation matrix including 17 variables. These data were measured on a 4 level likert scale.

# Details

# Autism:

- CI Circumscribed interests
- UP Unusual preoccupations
- RO Repetitive use of objects or interests in parts of objects
- CR Compulsions and/or rituals
- CI Unusual sensory interests
- SM Complex mannerisms or stereotyped body movements
- SU Stereotyped utterances/delayed echolalia
- NIL Neologisms and/or idiosyncratic language
- VR Verbal rituals

## OCD

- · CD Concern with things touched due to dirt/bacteria
- TB Thoughts of doing something bad around others
- CT Continual thoughts that do not go away
- HP Belief that someone/higher power put reoccurring thoughts in their head
- CW Continual washing
- CCh Continual checking CntCheck
- CC Continual counting/repeating
- RD Repeatedly do things until it feels good or just right

## bfi

## References

Jones, P. J., Ma, R., & McNally, R. J. (2019). Bridge centrality: A network approach to understanding comorbidity. Multivariate behavioral research, 1-15.

Ruzzano, L., Borsboom, D., & Geurts, H. M. (2015). Repetitive behaviors in autism and obsessivecompulsive disorder: New perspectives from a network analysis. Journal of Autism and Developmental Disorders, 45(1), 192-202. doi:10.1007/s10803-014-2204-9

## Examples

```
data("asd_ocd")
```

```
bfi
```

Data: 25 Personality items representing 5 factors

#### Description

This dataset and the corresponding documentation was taken from the **psych** package. We refer users to that package for further details (Revelle 2019).

## Usage

data("bfi")

#### Format

A data frame with 25 variables and 2800 observations (including missing values)

## Details

- A1 Am indifferent to the feelings of others. (q\_146)
- A2 Inquire about others' well-being. (q\_1162)
- A3 Know how to comfort others. (q\_1206)
- A4 Love children. (q\_1364)
- A5 Make people feel at ease. (q\_1419)
- C1 Am exacting in my work. (q\_124)
- C2 Continue until everything is perfect. (q\_530)
- C3 Do things according to a plan. (q\_619)

- C4 Do things in a half-way manner. (q\_626)
- C5 Waste my time. (q\_1949)
- E1 Don't talk a lot. (q\_712)
- E2 Find it difficult to approach others. (q\_901)
- E3 Know how to captivate people. (q\_1205)
- E4 Make friends easily. (q\_1410)
- E5 Take charge. (q\_1768)
- N1 Get angry easily. (q\_952)
- N2 Get irritated easily. (q\_974)
- N3 Have frequent mood swings. (q\_1099)
- N4 Often feel blue. (q\_1479)
- N5 Panic easily. (q\_1505)
- o1 Am full of ideas. (q\_128)
- o2 Avoid difficult reading material.(q\_316)
- o3 Carry the conversation to a higher level. (q\_492)
- o4 Spend time reflecting on things. (q\_1738)
- o5 Will not probe deeply into a subject. (q\_1964)
- gender Males = 1, Females =2
- education 1 = HS, 2 = finished HS, 3 = some college, 4 = college graduate 5 = graduate degree

## References

Revelle W (2019). *psych: Procedures for Psychological, Psychometric, and Personality Research*. Northwestern University, Evanston, Illinois. R package version 1.9.12, https://CRAN.R-project.org/package=psych.

bggm\_missing GGM: Missing Data

#### Description

Estimation and exploratory hypothesis testing with missing data.

## Usage

```
bggm_missing(x, iter = 2000, method = "estimate", ...)
```

#### bggm\_missing

#### Arguments

x	An object of class mid mice.
iter	Number of iterations for each imputed dataset (posterior samples; defaults to 2000).
method	Character string. Which method should be used (default set to estimate)? The current options are "estimate" and "explore".
	Additional arguments passed to either estimate or explore.

## Value

An object of class estimate or explore.

#### Note

Currently, **BGGM** is compatible with the package mice for handling the missing data. This is accomplished by fitting a model for each imputed dataset (i.e., more than one to account for uncertainty in the imputation step) and then pooling the estimates.

In a future version, an additional option will be added that allows for imputing the missing values during model fitting. This option will be incorporated directly into the estimate or explore functions, such that bggm\_missing will always support missing data with mice.

# Support:

There is limited support for missing data. As of version 2.0.0, it is possible to determine the graphical structure with either estimate or explore, in addition to plotting the graph with plot.select. All data types *are* currently supported.

**Memory Warning**: A model is fitted for each imputed dataset. This results in a potentially large object.

## Examples

```
# note: iter = 250 for demonstrative purposes
# need this package
library(mice, warn.conflicts = FALSE)
# data
Y <- ptsd[,1:5]
# matrix for indices
mat <- matrix(0, nrow = 221, ncol = 5)
# indices
indices <- which(mat == 0, arr.ind = TRUE)
# 50 NAs
Y[indices[sample(1:nrow(indices), 50),]] <- NA</pre>
```

# impute

```
x <- mice(Y, m = 5, print = FALSE)</pre>
####### copula #####
# rank based parital correlations
# estimate the model
fit_est <- bggm_missing(x,</pre>
                      method = "estimate",
                       type = "mixed",
                       iter = 250,
                       progress = FALSE)
# select edge set
E <- select(fit_est)</pre>
# plot E
plt_E <- plot(E)$plt</pre>
plt_E
```

coef.estimate Compute Regression Parameters for estimate Objects

## Description

There is a direct correspondence between the inverse covariance matrix and multiple regression (Kwan 2014; Stephens 1998). This readily allows for converting the GGM parameters to regression coefficients. All data types are supported.

## Usage

```
## S3 method for class 'estimate'
coef(object, iter = NULL, progress = TRUE, ...)
```

## Arguments

object	An Object of class estimate
iter	Number of iterations (posterior samples; defaults to the number in the object).
progress	Logical. Should a progress bar be included (defaults to TRUE)?
	Currently ignored.

## Value

An object of class coef, containing two lists.

- betas A list of length p, each containing a p 1 by iter matrix of posterior samples
- object An object of class estimate (the fitted model).

8

## coef.explore

#### References

Kwan CC (2014). "A regression-based interpretation of the inverse of the sample covariance matrix." *Spreadsheets in Education*, **7**(1), 4613.

Stephens G (1998). "On the Inverse of the Covariance Matrix in Portfolio Analysis." *The Journal of Finance*, **53**(5), 1821–1827.

#### Examples

```
# note: iter = 250 for demonstrative purposes
```

coef.explore

#### Compute Regression Parameters for explore Objects

### Description

There is a direct correspondence between the inverse covariance matrix and multiple regression (Kwan 2014; Stephens 1998). This readily allows for converting the GGM parameters to regression coefficients. All data types are supported.

## Usage

```
## S3 method for class 'explore'
coef(object, iter = NULL, progress = TRUE, ...)
```

#### Arguments

object	An Object of class explore.
iter	Number of iterations (posterior samples; defaults to the number in the object).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
	Currently ignored.

## Value

An object of class coef, containting two lists.

- betas A list of length p, each containing a p 1 by iter matrix of posterior samples
- object An object of class explore (the fitted model).

## References

Kwan CC (2014). "A regression-based interpretation of the inverse of the sample covariance matrix." *Spreadsheets in Education*, **7**(1), 4613.

Stephens G (1998). "On the Inverse of the Covariance Matrix in Portfolio Analysis." *The Journal of Finance*, **53**(5), 1821–1827.

#### Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- ptsd[,1:4]
### example 1: ordinal ###
# fit model (note + 1, due to zeros)
fit <- explore(Y + 1,</pre>
             type = "ordinal",
             iter = 250,
             progress = FALSE)
# summarize the partial correlations
reg <- coef(fit, progress = FALSE)</pre>
# summary
summ <- summary(reg)</pre>
summ
```

confirm

## Description

Confirmatory hypothesis testing in GGMs. Hypotheses are expressed as equality and/or ineqaulity contraints on the partial correlations of interest. Here the focus is *not* on determining the graph (see explore) but testing specific hypotheses related to the conditional (in)dependence structure. These methods were introduced in Williams and Mulder (2019).

# Usage

```
confirm(
 Y,
 hypothesis,
 prior_sd = 0.25,
 formula = NULL,
 type = "continuous",
 mixed_type = NULL,
 iter = 25000,
 progress = TRUE,
 impute = TRUE,
 seed = 1,
 ...
)
```

## Arguments

Υ	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables).
hypothesis	Character string. The hypothesis (or hypotheses) to be tested. See details.
prior_sd	Numeric. Scale of the prior distribution, approximately the standard deviation of a beta distribution (defaults to 0.25).
formula	An object of class formula. This allows for including control variables in the model (e.g.,, ~ gender * education).
type	Character string. Which type of data for <b>Y</b> ? The options include continuous, binary, ordinal, or mixed. See the note for further details.
mixed_type	Numeric vector of length $p$ . An indicator for which varibles should be treated as ranks. (1 for rank and 0 to assume normality). The default is currently (dev version) to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
iter	Number of iterations (posterior samples; defaults to 25,000).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
impute	Logicial. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) ?
seed	An integer for the random seed.
	Currently ignored.

#### Details

The hypotheses can be written either with the respective column names or numbers. For example, 1–-2 denotes the relation between the variables in column 1 and 2. Note that these must correspond to the upper triangular elements of the correlation matrix. This is accomplished by ensuring that the first number is smaller than the second number. This also applies when using column names (i.e., in reference to the column number).

## **One Hypothesis:**

To test whether some relations are larger than others, while others are expected to be equal, this can be writting as

• hyp <- c(1--2 > 1--3 = 1--4 > 0),

where there is an addition additional contraint that all effects are expected to be positive. This is then compared to the complement.

#### More Than One Hypothesis:

The above hypothesis can also be compared to, say, a null model by using ";" to seperate the hypotheses, for example,

• hyp <- c(1--2 > 1--3 = 1--4 > 0; 1--2 = 1--3 = 1--4 = 0).

Any number of hypotheses can be compared this way.

## Using "&"

It is also possible to include &. This allows for testing one constraint **and** another contraint as one hypothesis.

hyp <- c("A1--A2 > A1--A2 & A1--A3 = A1--A3")

Of course, it is then possible to include additional hypotheses by separating them with ";". Note also that the column names were used in this example (e.g., A1--A2 is the relation between those nodes).

## **Testing Sums**

It might also be interesting to test the sum of partial correlations. For example, that the sum of specific relations is larger than the sum of other relations. This can be written as

• hyp <- c("A1--A2 + A1--A3 > A1--A4 + A1--A5; A1--A2 + A1--A3 = A1--A4 + A1--A5")

#### **Potential Delays:**

There is a chance for a potentially long delay from the time the progress bar finishes to when the function is done running. This occurs when the hypotheses require further sampling to be tested, for example, when grouping relations c("(A1--A2, A1--A3) > (A1--A4, A1--A5)". This is not an error.

#### **Controlling for Variables:**

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

## 12

#### confirm

## Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables (Hoff 2007). This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed\_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

## **Dealing with Errors:**

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior\_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

## Value

The returned object of class confirm contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- out\_hyp\_prob Posterior hypothesis probabilities.
- info An object of class BF from the R package BFpack.

#### Note

#### "Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated (e.g., model selection consistency). That said, we would not consider this a "default" or "automatic" Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution.

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (relative to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

#### Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

## References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi:10.1214/07AOAS107.

Kass RE, Raftery AE (1995). "Bayes Factors." *Journal of the American Statistical Association*, **90**(430), 773–795.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi:10.31234/osf.io/ypxd8.

#### Examples

# note: iter = 250 for demonstrative purposes

```
### example 1: cheating ##
# Here a true hypothesis is tested,
# which shows the method works nicely
# (peeked at partials beforehand)
# data
Y <- BGGM::bfi[,1:10]
hypothesis <- c("A1--A2 < A1--A3 < A1--A4 = A1--A5")
# test cheat
test_cheat <- confirm(Y = Y,</pre>
                     type = "continuous",
                     hypothesis = hypothesis,
                     iter = 250,
                     progress = FALSE)
# print (probabilty of nearly 1 !)
test_cheat
```

constrained\_posterior Constrained Posterior Distribution

## Description

Compute the posterior distribution with off-diagonal elements of the precision matrix constrained to zero.

## constrained\_posterior

# Usage

```
constrained_posterior(
  object,
  adj,
  method = "direct",
  iter = 5000,
  progress = TRUE,
  ...
```

```
)
```

## Arguments

object	An object of class estimate or explore
adj	A p by p adjacency matrix. The zero entries denote the elements that should be constrained to zero.
method	Character string. Which method should be used ? Defaults to the "direct sampler" (i.e., method = "direct") described in page 122, section 2.4, Lenkoski (2013). The other option is a Metropolis-Hastings algorithm (MH). See details.
iter	Number of iterations (posterior samples; defaults to 5000).
progress	Logical. Should a progress bar be included (defaults to TRUE)?
	Currently ignored.

## Value

An object of class contrained, including

- precision\_mean The posterior mean for the precision matrix.
- pcor\_mean The posterior mean for the precision matrix.
- precision\_samps A 3d array of dimension p by p by iter including the sampled precision matrices.
- pcor\_samps A 3d array of dimension p by p by iter including sampled partial correlations matrices.

# References

Lenkoski A (2013). "A direct sampler for G-Wishart variates." Stat, 2(1), 119–128.

## Examples

```
# data
Y <- bfi[,1:10]
# sample posterior
fit <- estimate(Y, iter = 100)</pre>
```

convergence

MCMC Convergence

## Description

Monitor convergence of the MCMC algorithms.

## Usage

```
convergence(object, param = NULL, type = "trace", print_names = FALSE)
```

## Arguments

object	An object of class estimate or explore
param	Character string. Names of parameters for which to monitor MCMC convergence.
type	Character string. Which type of convergence plot ? The current options are trace (default) and acf.
print_names	Logical. Should the parameter names be printed (defaults to FALSE)? This can be used to first determine the parameter names to specify in type.

# Value

A list of ggplot objects.

## Note

An overview of MCMC diagnostics can be found here.

# Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- ptsd[,1:5]</pre>
```

16

```
CSWS
```

## Data: Contingencies of Self-Worth Scale (CSWS)

## Description

A dataset containing items from the Contingencies of Self-Worth Scale (CSWS) scale. There are 35 variables and 680 observations

## Usage

data("csws")

## Format

A data frame with 35 variables and 680 observations (7 point Likert scale)

## Details

- 1 When I think I look attractive, I feel good about myself
- 2 My self-worth is based on God's love
- 3 I feel worthwhile when I perform better than others on a task or skill.
- 4 My self-esteem is unrelated to how I feel about the way my body looks.
- 5 Doing something I know is wrong makes me lose my self-respect
- 6 I don't care if other people have a negative opinion about me.
- 7 Knowing that my family members love me makes me feel good about myself.
- 8 I feel worthwhile when I have God's love.
- 9 I can't respect myself if others don't respect me.
- 10 My self-worth is not influenced by the quality of my relationships with my family members.

- 11 Whenever I follow my moral principles, my sense of self-respect gets a boost.
- 12 Knowing that I am better than others on a task raises my self-esteem.
- 13 My opinion about myself isn't tied to how well I do in school.
- 14 I couldn't respect myself if I didn't live up to a moral code.
- 15 I don't care what other people think of me.
- 16 When my family members are proud of me, my sense of self-worth increases.
- 17 My self-esteem is influenced by how attractive I think my face or facial features are.
- 18 My self-esteem would suffer if I didn't have God's love.
- 19 Doing well in school gives me a sense of selfrespect.
- 20 Doing better than others gives me a sense of self-respect.
- 21 My sense of self-worth suffers whenever I think I don't look good.
- 22 I feel better about myself when I know I'm doing well academically.
- 23 What others think of me has no effect on what I think about myself.
- 24 When I don't feel loved by my family, my selfesteem goes down.
- 25 My self-worth is affected by how well I do when I am competing with others.
- 26 My self-esteem goes up when I feel that God loves me.
- 27 My self-esteem is influenced by my academic performance.
- 28 My self-esteem would suffer if I did something unethical.
- 29 It is important to my self-respect that I have a family that cares about me.
- 30 My self-esteem does not depend on whether or not I feel attractive.
- 31 When I think that I'm disobeying God, I feel bad about myself.
- 32 My self-worth is influenced by how well I do on competitive tasks.
- 33 I feel bad about myself whenever my academic performance is lacking.
- 34 My self-esteem depends on whether or not I follow my moral/ethical principles.
- 35 My self-esteem depends on the opinions others hold of me.
- gender "M" (male) or "F" (female)

## Note

There are seven domains

FAMILY SUPPORT: items 7, 10, 16, 24, and 29.
COMPETITION: items 3, 12, 20, 25, and 32.
APPEARANCE: items 1, 4, 17, 21, and 30.
GOD'S LOVE: items 2, 8, 18, 26, and 31.
ACADEMIC COMPETENCE: items 13, 19, 22, 27, and 33.
VIRTUE: items 5, 11, 14, 28, and 34.
APPROVAL FROM OTHERS: items: 6, 9, 15, 23, and 35.

## References

Briganti, G., Fried, E. I., & Linkowski, P. (2019). Network analysis of Contingencies of Self-Worth Scale in 680 university students. Psychiatry research, 272, 252-257.

#### Examples

data("csws")

depression\_anxiety\_t1 Data: Depression and Anxiety (Time 1)

## Description

A data frame containing 403 observations (n = 403) and 16 variables (p = 16) measured on the 4-point likert scale (depression: 9; anxiety: 7).

## Usage

```
data("depression_anxiety_t1")
```

#### Format

A data frame containing 403 observations (n = 7466) and 16 variables (p = 16) measured on the 4-point likert scale.

# Details

## Depression:

- PHQ1 Little interest or pleasure in doing things?
- PHQ2 Feeling down, depressed, or hopeless?
- PHQ3 Trouble falling or staying asleep, or sleeping too much?
- PHQ4 Feeling tired or having little energy?
- PHQ5 Poor appetite or overeating?
- PHQ6 Feeling bad about yourself or that you are a failure or have let yourself or your family down?
- PHQ7 Trouble concentrating on things, such as reading the newspaper or watching television?
- PHQ8 Moving or speaking so slowly that other people could have noticed? Or so fidgety or restless that you have been moving a lot more than usual?
- PHQ9 Thoughts that you would be better off dead, or thoughts of hurting yourself in some way?

#### Anxiety

- GAD1 Feeling nervous, anxious, or on edge
- · GAD2 Not being able to stop or control worrying
- · GAD3 Worrying too much about different things
- GAD4 Trouble relaxing
- GAD5 Being so restless that it's hard to sit still
- GAD6 Becoming easily annoyed or irritable
- · GAD7 Feeling afraid as if something awful might happen

#### References

Forbes, M. K., Baillie, A. J., & Schniering, C. A. (2016). A structural equation modeling analysis of the relationships between depression, anxiety, and sexual problems over time. The Journal of Sex Research, 53(8), 942-954.

Forbes, M. K., Wright, A. G., Markon, K. E., & Krueger, R. F. (2019). Quantifying the reliability and replicability of psychopathology network characteristics. Multivariate behavioral research, 1-19.

Jones, P. J., Williams, D. R., & McNally, R. J. (2019). Sampling variability is not nonreplication: a Bayesian reanalysis of Forbes, Wright, Markon, & Krueger.

## Examples

```
data("depression_anxiety_t1")
labels<- c("interest", "down", "sleep",
            "tired", "appetite", "selfest",
            "concen", "psychmtr", "suicid",
            "nervous", "unctrworry", "worrylot",
            "relax", "restless", "irritable", "awful")</pre>
```

depression\_anxiety\_t2 Data: Depression and Anxiety (Time 2)

## Description

A data frame containing 403 observations (n = 403) and 16 variables (p = 16) measured on the 4-point likert scale (depression: 9; anxiety: 7).

#### Usage

```
data("depression_anxiety_t2")
```

#### Format

A data frame containing 403 observations (n = 7466) and 16 variables (p = 16) measured on the 4-point likert scale.

## Details

#### Depression:

- PHQ1 Little interest or pleasure in doing things?
- PHQ2 Feeling down, depressed, or hopeless?
- PHQ3 Trouble falling or staying asleep, or sleeping too much?
- PHQ4 Feeling tired or having little energy?
- PHQ5 Poor appetite or overeating?
- PHQ6 Feeling bad about yourself or that you are a failure or have let yourself or your family down?
- PHQ7 Trouble concentrating on things, such as reading the newspaper or watching television?
- PHQ8 Moving or speaking so slowly that other people could have noticed? Or so fidgety or restless that you have been moving a lot more than usual?
- PHQ9 Thoughts that you would be better off dead, or thoughts of hurting yourself in some way?

## Anxiety

- GAD1 Feeling nervous, anxious, or on edge
- GAD2 Not being able to stop or control worrying
- GAD3 Worrying too much about different things
- GAD4 Trouble relaxing
- GAD5 Being so restless that it's hard to sit still
- GAD6 Becoming easily annoyed or irritable
- GAD7 Feeling afraid as if something awful might happen

#### References

Forbes, M. K., Baillie, A. J., & Schniering, C. A. (2016). A structural equation modeling analysis of the relationships between depression, anxiety, and sexual problems over time. The Journal of Sex Research, 53(8), 942-954.

Forbes, M. K., Wright, A. G., Markon, K. E., & Krueger, R. F. (2019). Quantifying the reliability and replicability of psychopathology network characteristics. Multivariate behavioral research, 1-19.

Jones, P. J., Williams, D. R., & McNally, R. J. (2019). Sampling variability is not nonreplication: a Bayesian reanalysis of Forbes, Wright, Markon, & Krueger.

# Examples

```
data("depression_anxiety_t2")
labels<- c("interest", "down", "sleep",
                "tired", "appetite", "selfest",
                "concen", "psychmtr", "suicid",
                "nervous", "unctrworry", "worrylot",
                "relax", "restless", "irritable", "awful")</pre>
```

## Description

Estimate the conditional (in)dependence with either an analytic solution or efficiently sampling from the posterior distribution. These methods were introduced in Williams (2018). The graph is selected with select.estimate and then plotted with plot.select.

# Usage

```
estimate(
    Y,
    formula = NULL,
    type = "continuous",
    mixed_type = NULL,
    analytic = FALSE,
    prior_sd = 0.25,
    iter = 5000,
    impute = FALSE,
    progress = TRUE,
    seed = 1,
    ...
)
```

## Arguments

Y	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables).
formula	An object of class formula. This allows for including control variables in the model (i.e., ~ gender). See the note for further details.
type	Character string. Which type of data for Y? The options include continuous, binary, ordinal, or mixed. Note that mixed can be used for data with only ordinal variables. See the note for further details.
mixed_type	Numeric vector. An indicator of length $p$ for which variables should be treated as ranks. (1 for rank and 0 to assume normality). The default is currently to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
analytic	Logical. Should the analytic solution be computed (default is FALSE)?
prior_sd	Scale of the prior distribution, approximately the standard deviation of a beta distribution (defaults to 0.50).
iter	Number of iterations (posterior samples; defaults to 5000).
impute	Logical. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$
progress	Logical. Should a progress bar be included (defaults to TRUE)?
seed	An integer for the random seed.
	Currently ignored.

#### Details

The default is to draw samples from the posterior distribution (analytic = FALSE). The samples are required for computing edge differences (see ggm\_compare\_estimate), Bayesian R2 introduced in Gelman et al. (2019) (see predictability), etc. If the goal is to \*only\* determine the non-zero effects, this can be accomplished by setting analytic = TRUE. This is particularly useful when a fast solution is needed (see the examples in ggm\_compare\_ppc)

## **Controlling for Variables:**

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

## Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option  $mixed_type$  allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise (Hoff 2007). This is accomplished by specifying an indicator vector of length p. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are treated as ranks.

#### **Dealing with Errors:**

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior\_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

#### **Imputing Missing Values:**

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

## Value

The returned object of class estimate contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- pcor\_mat Partial correlation matrix (posterior mean).
- post\_samp An object containing the posterior samples.

#### Note

## **Posterior Uncertainty:**

A key feature of **BGGM** is that there is a posterior distribution for each partial correlation. This readily allows for visibalizing uncertainty in the estimates. This feature works with all data types and is accomplished by plotting the summary of the estimate object (i.e., plot(summary(fit))). Several examples are provided below.

### Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

#### References

Gelman A, Goodrich B, Gabry J, Vehtari A (2019). "R-squared for Bayesian Regression Models." *American Statistician*, **73**(3), 307–309. ISSN 15372731, doi:10.1080/00031305.2018.1549100.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi:10.1214/07AOAS107.

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi:10.31234/OSF.IO/X8DPR.

## Examples

```
# note: iter = 250 for demonstrative purposes
```

```
# select the graph
E <- select(fit)</pre>
# plot the selected graph
plt_E <- plot(select(fit))</pre>
# ordinal
# fit model (note + 1, due to zeros)
fit <- estimate(Y + 1, type = "ordinal",</pre>
               iter = 250)
# summarize the partial correlations
summ <- summary(fit)</pre>
# plot the summary
plt <- plot(summary(fit))</pre>
# select the graph
E <- select(fit)</pre>
# plot the selected graph
plt_E <- plot(select(fit))</pre>
****
## example 2: analytic solution ##
# (only continuous)
# data
Y <- ptsd
# fit model
fit <- estimate(Y, analytic = TRUE)</pre>
# summarize the partial correlations
summ <- summary(fit)</pre>
# plot summary
plt_summ <- plot(summary(fit))</pre>
# select graph
E <- select(fit)</pre>
# plot the selected graph
```

plt\_E <- plot(select(fit))</pre>

#### explore

## Description

Learn the conditional (in)dependence structure with the Bayes factor using the matrix-F prior distribution (Mulder and Pericchi 2018). These methods were introduced in Williams and Mulder (2019). The graph is selected with select.explore and then plotted with plot.select.

## Usage

```
explore(
    Y,
    formula = NULL,
    type = "continuous",
    mixed_type = NULL,
    analytic = FALSE,
    prior_sd = 0.25,
    iter = 5000,
    progress = TRUE,
    impute = FALSE,
    seed = 1,
    ...
)
```

#### Arguments

Y	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables).
formula	An object of class formula. This allows for including control variables in the model (i.e., ~ gender).
type	Character string. Which type of data for Y ? The options include continuous, binary, ordinal, or mixed (semi-parametric copula). See the note for further details.
mixed_type	Numeric vector. An indicator of length p for which varibles should be treated as ranks. (1 for rank and 0 to assume normality). The default is to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
analytic	Logical. Should the analytic solution be computed (default is FALSE)? (currently not implemented)
prior_sd	Scale of the prior distribution, approximately the standard deviation of a beta distribution (defaults to $0.25$ ).
iter	Number of iterations (posterior samples; defaults to 5000).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
impute	Logicial. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$

#### explore

seed	An integer for the random seed.
	Currently ignored (leave empty).

#### Details

#### **Controlling for Variables:**

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

#### Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed\_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

## Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior\_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

#### **Imputing Missing Values:**

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

## Value

The returned object of class explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- pcor\_mat partial correlation matrix (posterior mean).
- post\_samp an object containing the posterior samples.

## **Posterior Uncertainty:**

A key feature of **BGGM** is that there is a posterior distribution for each partial correlation. This readily allows for visiualizing uncertainty in the estimates. This feature works with all data types and is accomplished by plotting the summary of the explore object (i.e., plot(summary(fit))). Note that in contrast to estimate (credible intervals), the posterior standard deviation is plotted for explore objects.

## "Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated including model selection consistency. That said, we would not consider this a "default" (or "automatic") Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution.

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (**relative** to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

#### Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

#### References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

Kass RE, Raftery AE (1995). "Bayes Factors." *Journal of the American Statistical Association*, **90**(430), 773–795.

Mulder J, Pericchi L (2018). "The Matrix-F Prior for Estimating and Testing Covariance Matrices." *Bayesian Analysis*, 1–22. ISSN 19316690, doi:10.1214/17BA1092.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi:10.31234/osf.io/ypxd8.

## Examples

# note: iter = 250 for demonstrative purposes

# fit model

# Note

## fisher\_r\_to\_z

fisher\_r\_to\_z Fisher Z Transformation

# Description

Tranform correlations to Fisher's Z

## Usage

```
fisher_r_to_z(r)
```

## Arguments

r correlation (can be a vector)

# Value

Fisher Z transformed correlation(s)

## Examples

fisher\_r\_to\_z(0.5)

fisher\_z\_to\_r

## Description

Back tranform Fisher's Z to correlations

## Usage

fisher\_z\_to\_r(z)

# Arguments

z Fisher Z

## Value

Correlation (s) (backtransformed)

## Examples

fisher\_z\_to\_r(0.5)

gen\_net

## Simulate a Partial Correlation Matrix

# Description

Simulate a Partial Correlation Matrix

# Usage

gen\_net(p = 20, edge\_prob = 0.3, 1b = 0.05, ub = 0.3)

## Arguments

р	number of variables (nodes)
edge_prob	connectivity
lb	lower bound for the partial correlations
ub	upper bound for the partial correlations

## gen\_ordinal

## Value

A list containing the following:

- pcor: Partial correlation matrix, encoding the conditional (in)dependence structure.
- cors: Correlation matrix.
- adj: Adjacency matrix.
- trys: Number of attempts to obtain a positive definite matrix.

## Note

The function checks for a valid matrix (positive definite), but sometimes this will still fail. For example, for larger p, to have large partial correlations this requires a sparse GGM (accomplished by setting edge\_prob to a small value).

### Examples

```
true_net <- gen_net(p = 10)</pre>
```

gen\_ordinal Generate Ordinal and Binary data

## Description

Generate Multivariate Ordinal and Binary data.

### Usage

```
gen_ordinal(n, p, levels = 2, cor_mat, empirical = FALSE)
```

## Arguments

n	Number of observations ( <i>n</i> ).
р	Number of variables ( <i>p</i> ).
levels	Number of categories (defaults to 2; binary data).
cor_mat	A p by p matrix including the true correlation structure.
empirical	Logical. If true, cor_mat specifies the empirical not population covariance matrix.

#### Value

A *n* by *p* data matrix.

In order to allow users to enjoy the functionality of **BGGM**, we had to make minor changes to the function rmvord\_naiv from the R package **orddata** (Leisch et al. 2010). All rights to, and credit for, the function rmvord\_naiv belong to the authors of that package.

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#### References

Leisch F, Kaiser AWS, Hornik K (2010). *orddata: Generation of Artificial Ordinal and Binary Data*. R package version 0.1/r4, https://R-Forge.R-project.org/projects/orddata/.

## Examples

```
main <- ptsd_cor1[1:5,1:5]</pre>
p <- ncol(main)</pre>
pcors <- -(cov2cor(solve(main)) -diag(p))</pre>
diag(pcors) < -1
pcors <- ifelse(abs(pcors) < 0.05, 0, pcors)</pre>
inv <- -pcors</pre>
diag(inv) < -1
cors <- cov2cor( solve(inv))</pre>
# example data
Y \leq BGGM::gen_ordinal(n = 500, p = 5,
                 levels = 2,
                 cor_mat = cors,
                 empirical = FALSE)
# empirical = TRUE
Y <- gen_ordinal(n = 500,
             p = 16,
             levels = 5,
             cor_mat = ptsd_cor1,
             empirical = TRUE)
```

32

# Note

ggm\_compare\_confirm GGM Compare: Confirmatory Hypothesis Testing

## Description

Confirmatory hypothesis testing for comparing GGMs. Hypotheses are expressed as equality and/or ineqaulity contraints on the partial correlations of interest. Here the focus is *not* on determining the graph (see explore) but testing specific hypotheses related to the conditional (in)dependence structure. These methods were introduced in Williams and Mulder (2019) and in Williams et al. (2020)

## Usage

```
ggm_compare_confirm(
...,
hypothesis,
formula = NULL,
type = "continuous",
mixed_type = NULL,
prior_sd = 0.25,
iter = 25000,
impute = TRUE,
progress = TRUE,
seed = 1
)
```

## Arguments

	At least two matrices (or data frame) of dimensions $n$ (observations) by $p$ (nodes).
hypothesis	Character string. The hypothesis (or hypotheses) to be tested. See notes for futher details.
formula	an object of class formula. This allows for including control variables in the model (i.e., ~ gender).
type	Character string. Which type of data for Y ? The options include continuous, binary, ordinal, or mixed. Note that mixed can be used for data with only ordinal variables. See the note for further details.
mixed_type	numeric vector. An indicator of length p for which varibles should be treated as ranks. (1 for rank and 0 to assume normality). The default is currently (dev version) to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
prior_sd	Numeric. The scale of the prior distribution (centered at zero), in reference to a beta distribution (defaults to 0.25).
iter	Number of iterations (posterior samples; defaults to 25,000).

impute	Logicial. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
seed	An integer for the random seed.

## Details

The hypotheses can be written either with the respective column names or numbers. For example,  $g1_1-2$  denotes the relation between the variables in column 1 and 2 for group 1. The  $g1_i$  is required and the only difference from confirm (one group). Note that these must correspond to the upper triangular elements of the correlation matrix. This is accomplished by ensuring that the first number is smaller than the second number. This also applies when using column names (i.e., in reference to the column number).

#### **One Hypothesis:**

To test whether a relation in larger in one group, while both are expected to be positive, this can be written as

hyp <- c(g1\_1--2 > g2\_1--2 > 0)

This is then compared to the complement.

#### More Than One Hypothesis:

The above hypothesis can also be compared to, say, a null model by using ";" to seperate the hypotheses, for example,

• hyp <- c(g1\_1--2 > g2\_1--2 > 0; g1\_1--2 = g2\_1--2 = 0).

Any number of hypotheses can be compared this way.

#### Using "&"

It is also possible to include &. This allows for testing one constraint **and** another contraint as one hypothesis.

hyp <- c("g1\_A1--A2 > g2\_A1--A2 & g1\_A1--A3 = g2\_A1--A3")

Of course, it is then possible to include additional hypotheses by separating them with ";".

## **Testing Sums**

It might also be interesting to test the sum of partial correlations. For example, that the sum of specific relations in one group is larger than the sum in another group.

hyp <- c("g1\_A1--A2 + g1\_A1--A3 > g2\_A1--A2 + g2\_A1--A3; g1\_A1--A2 + g1\_A1--A3 = g2\_A1--A2 + g2\_A1--A3")

#### **Potential Delays:**

There is a chance for a potentially long delay from the time the progress bar finishes to when the function is done running. This occurs when the hypotheses require further sampling to be tested, for example, when grouping relations  $c("(g1_A1-A2, g2_A2-A3) > (g2_A1-A2, g2_A2-A3)"$ . This is not an error.

#### **Controlling for Variables:**

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

#### Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables (Hoff 2007). This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed\_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

#### **Dealing with Errors:**

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior\_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

#### **Imputing Missing Values:**

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

## Value

The returned object of class confirm contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- out\_hyp\_prob Posterior hypothesis probabilities.
- info An object of class BF from the R package BFpack (Mulder et al. 2019)

#### "Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated (e.g., model selection consistency). That said, we would not consider this a "default" or "automatic" Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution (prior\_sd).

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (relative to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

## Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

#### References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi:10.1214/07AOAS107.

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

Kass RE, Raftery AE (1995). "Bayes Factors." *Journal of the American Statistical Association*, **90**(430), 773–795.

Mulder J, Gu X, Olsson-Collentine A, Tomarken A, Böing-Messing F, Hoijtink H, Meijerink M, Williams DR, Menke J, Fox J, others (2019). "BFpack: Flexible Bayes Factor Testing of Scientific Theories in R." *arXiv preprint arXiv:1911.07728*.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi:10.31234/osf.io/ypxd8.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*. doi:10.1037/met0000254.

#### Examples

36

Note

```
# males
Ymale <- subset(Y, gender == 1,</pre>
                select = -c(education,
                           gender))[,1:5]
# females
Yfemale <- subset(Y, gender == 2,</pre>
                   select = -c(education,
                              gender))[,1:5]
# exhaustive
hypothesis <- c("g1_A1-A2 > g2_A1-A2;
                g1_A1--A2 < g2_A1--A2;
                g1_A1 - A2 = g2_A1 - A2")
# test hyp
test <- ggm_compare_confirm(Ymale, Yfemale,</pre>
                         hypothesis = hypothesis,
                         iter = 250,
                         progress = FALSE)
# print (evidence not strong)
test
*****
#### example 2: sensitivity to prior ####
*****
# continued from example 1
# decrease prior SD
test <- ggm_compare_confirm(Ymale,</pre>
                         Yfemale,
                         prior_sd = 0.1,
                         hypothesis = hypothesis,
                         iter = 250,
                         progress = FALSE)
# print
test
# indecrease prior SD
test <- ggm_compare_confirm(Ymale,</pre>
                         Yfemale,
                         prior_sd = 0.5,
                         hypothesis = hypothesis,
                         iter = 250,
                         progress = FALSE)
# print
```

test

```
#### example 3: mixed data #####
hypothesis <- c("g1_A1-A2 > g2_A1-A2;
             g1_A1 - A2 < g2_A1 - A2;
             g1_A1 - A2 = g2_A1 - A2")
# test (1000 for example)
test <- ggm_compare_confirm(Ymale,</pre>
                      Yfemale,
                      type = "mixed",
                      hypothesis = hypothesis,
                      iter = 250,
                      progress = FALSE)
# print
test
##### example 4: control #####
# control for education
# data
Y <- bfi
# males
Ymale <- subset(Y, gender == 1,</pre>
              select = -c(gender))[,c(1:5, 26)]
# females
Yfemale <- subset(Y, gender == 2,</pre>
              select = -c(gender))[,c(1:5, 26)]
# test
test <- ggm_compare_confirm(Ymale,</pre>
                       Yfemale,
                       formula = ~ education,
                       hypothesis = hypothesis,
                       iter = 250,
                       progress = FALSE)
# print
test
##### example 5: many relations #####
# data
Y <- bfi
```

```
hypothesis <- c("g1_A1--A2 > g2_A1--A2 & g1_A1--A3 = g2_A1--A3;
                 g1_A1--A2 = g2_A1--A2 & g1_A1--A3 = g2_A1--A3;
                 g1_A1--A2 = g2_A1--A2 = g1_A1--A3 = g2_A1--A3")
Ymale
        <- subset(Y, gender == 1,
                  select = -c(education,
                               gender))[,1:5]
# females
Yfemale <- subset(Y, gender == 2,</pre>
                      select = -c(education,
                                  gender))[,1:5]
test <- ggm_compare_confirm(Ymale,</pre>
                             Yfemale,
                              hypothesis = hypothesis,
                              iter = 250,
                              progress = FALSE)
# print
test
```

ggm\_compare\_estimate GGM Compare: Estimate

### Description

Compare partial correlations that are estimated from any number of groups. This method works for continuous, binary, ordinal, and mixed data (a combination of categorical and continuous variables). The approach (i.e., a difference between posterior distributions) was described in Williams (2018).

#### Usage

```
ggm_compare_estimate(
...,
formula = NULL,
type = "continuous",
mixed_type = NULL,
analytic = FALSE,
prior_sd = 0.5,
iter = 5000,
impute = TRUE,
progress = TRUE,
seed = 1
```

#### Arguments

	Matrices (or data frames) of dimensions $n$ (observations) by $p$ (variables). Requires at least two.
formula	An object of class formula. This allows for including control variables in the model (i.e., ~ gender). See the note for further details.
type	Character string. Which type of data for <b>Y</b> ? The options include continuous, binary, ordinal, or continuous. See the note for further details.
<pre>mixed_type</pre>	Numeric vector. An indicator of length $p$ for which varibles should be treated as ranks. (1 for rank and 0 to use the 'empirical' or observed distribution). The default is currently to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
analytic	Logical. Should the analytic solution be computed (default is FALSE)? This is only available for continous data. Note that if type = "mixed" and analytic = TRUE, the data will automatically be treated as continuous.
prior_sd	The scale of the prior distribution (centered at zero), in reference to a beta dis- tribution (defaults to 0.50). See note for further details.
iter	Number of iterations (posterior samples; defaults to 5000).
impute	Logicial. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
seed	An integer for the random seed.

### Details

This function can be used to compare the partial correlations for any number of groups. This is accomplished with pairwise comparisons for each relation. In the case of three groups, for example, group 1 and group 2 are compared, then group 1 and group 3 are compared, and then group 2 and group 3 are compared. There is a full distibution for each difference that can be summarized (i.e., summary.ggm\_compare\_estimate) and then visualized (i.e., plot.summary.ggm\_compare\_estimate). The graph of difference is selected with select.ggm\_compare\_estimate).

### **Controlling for Variables:**

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

## Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed\_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector

of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

#### **Dealing with Errors:**

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior\_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

#### **Imputing Missing Values:**

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

### Value

A list of class ggm\_compare\_estimate containing:

- pcor\_diffs partial correlation differences (posterior distribution)
- p number of variable
- info list containing information about each group (e.g., sample size, etc.)
- iter number of posterior samples
- call match.call

#### Note

### Mixed Data:

The mixed data approach was introduced in Hoff (2007) (our paper describing an extension to Bayesian hypothesis testing if forthcoming). This is a semi-paramateric copula model based on the ranked likelihood. This is computationally expensive when treating continuous data as ranks. The current default is to treat only integer data as ranks. This should of course be adjusted for continuous data that is skewed. This can be accomplished with the argument mixed\_type. A 1 in the numeric vector of length *p*indicates to treat that respective node as a rank (corresponding to the column number) and a zero indicates to use the observed (or "emprical") data.

It is also important to note that type = "mixed" is not restricted to mixed data (containing a combination of categorical and continuous): all the nodes can be ordinal or continuous (but again this will take some time).

#### Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

#### **Additional GGM Compare Methods**

Bayesian hypothesis testing is implemented in ggm\_compare\_explore and ggm\_compare\_confirm (Williams and Mulder 2019). The latter allows for confirmatory hypothesis testing. An approach based on a posterior predictive check is implemented in ggm\_compare\_ppc (Williams et al. 2020). This provides a 'global' test for comparing the entire GGM and a 'nodewise' test for comparing each variable in the network Williams (2018).

#### References

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi:10.1214/07AOAS107.

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi:10.31234/OSF.IO/X8DPR.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi:10.31234/osf.io/ypxd8.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*. doi:10.1037/met0000254.

## Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                    select = -c(gender,
                                 education))[,1:10]
Yfemale <- subset(Y, gender == 2,</pre>
                      select = -c(gender),
                                   education))[,1:10]
# fit model
fit <- ggm_compare_estimate(Ymale, Yfemale,</pre>
                             type = "ordinal",
                             iter = 250,
                             prior_sd = 0.25,
                             progress = FALSE)
```

42

ggm\_compare\_explore GGM Compare: Exploratory Hypothesis Testing

### Description

Compare Gaussian graphical models with exploratory hypothesis testing using the matrix-F prior distribution (Mulder and Pericchi 2018). A test for each partial correlation in the model for any number of groups. This provides evidence for the null hypothesis of no difference and the alternative hypothesis of difference. With more than two groups, the test is for *all* groups simultaneously (i.e., the relation is the same or different in all groups). This method was introduced in Williams et al. (2020). For confirmatory hypothesis testing see confirm\_groups.

### Usage

```
ggm_compare_explore(
...,
formula = NULL,
type = "continuous",
mixed_type = NULL,
analytic = FALSE,
prior_sd = 0.2,
iter = 5000,
progress = TRUE,
seed = 1
)
```

#### Arguments

	At least two matrices (or data frame) of dimensions $n$ (observations) by $p$ (variables).
formula	An object of class formula. This allows for including control variables in the model (i.e., ~ gender).
type	Character string. Which type of data for Y ? The options include continuous, binary, or ordinal. See the note for further details.
<pre>mixed_type</pre>	Numeric vector. An indicator of length p for which varibles should be treated as ranks. (1 for rank and 0 to assume normality). The default is currently (dev version) to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
analytic	logical. Should the analytic solution be computed (default is FALSE)? See note for details.
prior_sd	Numeric. The scale of the prior distribution (centered at zero), in reference to a beta distribution. The 'default' is 0.20. See note for further details.
iter	number of iterations (posterior samples; defaults to 5000).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
seed	An integer for the random seed.

### Details

### **Controlling for Variables:**

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

## Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed\_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

### **Dealing with Errors:**

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

• The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior\_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.

• The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

#### Value

The returned object of class ggm\_compare\_explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- BF\_01 A p by p matrix including the Bayes factor for the null hypothesis.
- pcor\_diff A p by p matrix including the difference in partial correlations (only for two groups).
- samp A list containing the fitted models (of class explore) for each group.

#### Note

#### "Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated, such model selection consistency. That said, we would not consider this a "default" Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution.

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (relative to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

#### Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

#### References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Kass RE, Raftery AE (1995). "Bayes Factors." *Journal of the American Statistical Association*, **90**(430), 773–795.

Mulder J, Pericchi L (2018). "The Matrix-F Prior for Estimating and Testing Covariance Matrices." *Bayesian Analysis*, 1–22. ISSN 19316690, doi:10.1214/17BA1092.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi:10.31234/osf.io/ypxd8.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*. doi:10.1037/met0000254.

## Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                  select = -c(gender,
                              education))[,1:10]
Yfemale <- subset(Y, gender == 2,</pre>
                    select = -c(gender),
                                education))[,1:10]
### example 1: ordinal ###
# fit model
fit <- ggm_compare_explore(Ymale, Yfemale,</pre>
                          type = "ordinal",
                          iter = 250,
                          progress = FALSE)
# summary
summ <- summary(fit)</pre>
# edge set
E <- select(fit)</pre>
```

ggm\_compare\_ppc

GGM Compare: Posterior Predictive Check

### Description

Compare GGMs with a posterior predicitve check (Gelman et al. 1996). This method was introduced in Williams et al. (2020). Currently, there is a global (the entire GGM) and a nodewise test. The default is to compare GGMs with respect to the posterior predictive distribution of Kullback Leibler divergence and the sum of squared errors. It is also possible to compare the GGMs with a user defined test-statistic.

#### Usage

```
ggm_compare_ppc(
    ...,
```

#### ggm\_compare\_ppc

```
test = "global",
iter = 5000,
FUN = NULL,
custom_obs = NULL,
loss = TRUE,
progress = TRUE
```

# )

## Arguments

	At least two matrices (or data frames) of dimensions $n$ (observations) by $p$ (variables).
test	Which test should be performed (defaults to "global") ? The options include global and nodewise.
iter	Number of replicated datasets used to construct the predictivie distribution (defaults to 5000).
FUN	An optional function for comparing GGMs that returns a number. See <b>Details</b> .
custom_obs	Number corresponding to the observed score for comparing the GGMs. This is required if a function is provided in FUN. See <b>Details</b> .
loss	Logical. If a function is provided, is the measure a "loss function" (i.e., a large score is bad thing). This determines how the <i>p</i> -value is computed. See <b>Details</b> .
progress	Logical. Should a progress bar be included (defaults to TRUE) ?

### Details

The FUN argument allows for a user defined test-statisic (the measure used to compare the GGMs). The function must include only two agruments, each of which corresponds to a dataset. For example, f <- function(Yg1, Yg2), where each Y is dataset of dimensions *n* by *p*. The groups are then compare within the function, returning a single number. An example is provided below.

Further, when using a custom function care must be taken when specifying the argument loss. We recommended to visualize the results with plot to ensure the *p*-value was computed in the right direction.

### Value

The returned object of class ggm\_compare\_ppc contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

test = "global"

- ppp\_jsd posterior predictive *p*-values (JSD).
- ppp\_sse posterior predictive *p*-values (SSE).
- predictive\_jsd list containing the posterior predictive distributions (JSD).
- predictive\_sse list containing the posterior predictive distributions (SSE).
- obs\_jsd list containing the observed error (JSD).
- obs\_sse list containing the observed error (SSE).

test = "nodewise"

- ppp\_jsd posterior predictive *p*-values (JSD).
- predictive\_jsd list containing the posterior predictive distributions (JSD).
- obs\_jsd list containing the observed error (JSD).

FUN = f()

- ppp\_custom posterior predictive *p*-values (custom).
- predictive\_custom posterior predictive distributions (custom).
- obs\_custom observed error (custom).

#### Note

# Interpretation:

The primary test-statistic is symmetric KL-divergence that is termed Jensen-Shannon divergence (JSD). This is in essence a likelihood ratio that provides the "distance" between two multivariate normal distributions. The basic idea is to (1) compute the posterior predictive distribution, assuming group equality (the null model). This provides the error that we would expect to see under the null model; (2) compute JSD for the observed groups; and (3) compare the observed JSD to the posterior predictive distribution, from which a posterior predictive *p*-value is computed.

For the global check, the sum of squared error is also provided. This is computed from the partial correlation matrices and it is analagous to the strength test in van Borkulo et al. (2017). The nodewise test compares the posterior predictive distribution for each node. This is based on the correspondence between the inverse covariance matrix and multiple regression (Kwan 2014; Stephens 1998).

If the null model is not rejected, note that this does not provide evidence for equality! Further, if the null model is rejected, this means that the assumption of group equality is not tenable–the groups are different.

#### **Alternative Methods:**

There are several methods in **BGGM** for comparing groups. See ggm\_compare\_estimate (posterior differences for the partial correlations), ggm\_compare\_explore (exploratory hypothesis testing), and ggm\_compare\_confirm (confirmatory hypothesis testing).

### References

Gelman A, Meng X, Stern H (1996). "Posterior predictive assessment of model fitness via realized discrepancies." *Statistica sinica*, 733–760.

Kwan CC (2014). "A regression-based interpretation of the inverse of the sample covariance matrix." *Spreadsheets in Education*, 7(1), 4613.

Stephens G (1998). "On the Inverse of the Covariance Matrix in Portfolio Analysis." *The Journal of Finance*, **53**(5), 1821–1827.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*.

48

#### doi:10.1037/met0000254.

van Borkulo CD, Boschloo L, Kossakowski J, Tio P, Schoevers RA, Borsboom D, Waldorp LJ (2017). "Comparing network structures on three aspects: A permutation test." *Manuscript submitted for publication*.

## Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males
Ym <- subset(Y, gender == 1,</pre>
          select = - c(gender, education))
# females
Yf \leq subset(Y, gender == 2,
          select = - c(gender, education))
global_test <- ggm_compare_ppc(Ym, Yf,</pre>
                         iter = 250)
global_test
###### custom function ######
# example 1
# maximum difference van Borkulo et al. (2017)
f <- function(Yg1, Yg2){</pre>
# remove NA
x <- na.omit(Yg1)</pre>
y <- na.omit(Yg2)</pre>
# nodes
p <- ncol(Yg1)</pre>
```

```
# identity matrix
I_p <- diag(p)</pre>
# partial correlations
pcor_1 <- -(cov2cor(solve(cor(x))) - I_p)</pre>
pcor_2 <- -(cov2cor(solve(cor(y))) - I_p)</pre>
# max difference
max(abs((pcor_1[upper.tri(I_p)] - pcor_2[upper.tri(I_p)])))
}
# observed difference
obs <- f(Ym, Yf)
global_max <- ggm_compare_ppc(Ym, Yf,</pre>
                                 iter = 250,
                                 FUN = f,
                                 custom_obs = obs,
                                 progress = FALSE)
global_max
# example 2
# Hamming distance (squared error for adjacency)
f <- function(Yg1, Yg2){</pre>
# remove NA
x <- na.omit(Yg1)</pre>
y <- na.omit(Yg2)</pre>
# nodes
p <- ncol(x)
# identity matrix
I_p <- diag(p)</pre>
fit1 <- estimate(x, analytic = TRUE)</pre>
fit2 <- estimate(y, analytic = TRUE)</pre>
sel1 <- select(fit1)</pre>
sel2 <- select(fit2)</pre>
sum((sel1$adj[upper.tri(I_p)] - sel2$adj[upper.tri(I_p)])^2)
}
# observed difference
obs <- f(Ym, Yf)
```

50

gss

gss

#### Data: 1994 General Social Survey

## Description

A data frame containing 1002 rows and 7 variables measured on various scales, including binary and ordered cateogrical (with varying numbers of categories). There are also missing values in each variable

- Inc Income of the respondent in 1000s of dollars, binned into 21 ordered categories.
- DEG Highest degree ever obtained (none, HS, Associates, Bachelors, or Graduate)
- CHILD Number of children ever had.
- PINC Financial status of respondent's parents when respondent was 16 (on a 5-point scale).
- · PDEG Maximum of mother's and father's highest degree
- · PCHILD Number of siblings of the respondent plus one
- AGE Age of the respondent in years.

### Usage

data("gss")

## Format

A data frame containing 1190 observations (n = 1190) and 6 variables (p = 6) measured on the binary scale (Fowlkes et al. 1988). The variable descriptions were copied from section 4, Hoff (2007)

52

### References

Fowlkes EB, Freeny AE, Landwehr JM (1988). "Evaluating logistic models for large contingency tables." *Journal of the American Statistical Association*, **83**(403), 611–622. doi:10.1080/ 01621459.1988.10478640.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi:10.1214/07AOAS107.

### Examples

data("gss")

ifit

Data: ifit Intensive Longitudinal Data

#### Description

A data frame containing 8 variables and nearly 200 observations. There are two subjects, each of which provided data every data for over 90 days. Six variables are from the PANAS scale (positive and negative affect), the daily number of steps, and the subject id.

- · id Subject id
- interested
- disinterested
- excited
- upset
- strong
- stressed
- steps steps recorded by a fit bit

#### Usage

data("ifit")

#### Format

A data frame containing 197 observations and 8 variables. The data have been used in (O'Laughlin et al. 2020) and (Williams et al. 2019)

### References

O'Laughlin KD, Liu S, Ferrer E (2020). "Use of Composites in Analysis of Individual Time Series: Implications for Person-Specific Dynamic Parameters." *Multivariate Behavioral Research*, 1–18. doi:10.1080/00273171.2020.1716673.

Williams DR, Liu S, Martin SR, Rast P (2019). "Bayesian Multivariate Mixed-Effects Location Scale Modeling of Longitudinal Relations among Affective Traits, States, and Physical Activity." *PsyArXiv.* doi:10.31234/osf.io/4kfjp.

## impute\_data

### Examples

data("ifit")

impute\_data Obtain Imputed Datasets

### Description

Impute missing values, assuming a multivariate normal distribution, with the posterior predictive distribution. For binary, ordinal, and mixed (a combination of discrete and continuous) data, the values are first imputed for the latent data and then converted to the original scale.

### Usage

```
impute_data(
   Y,
   type = "continuous",
   lambda = NULL,
   mixed_type = NULL,
   iter = 1000,
   progress = TRUE
)
```

# Arguments

Υ	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables).
type	Character string. Which type of data for Y? The options include continuous, binary, ordinal, or mixed. Note that mixed can be used for data with only ordinal variables. See the note for further details.
lambda	Numeric. A regularization parameter, which defaults to $p + 2$ . A larger value results in more shrinkage.
<pre>mixed_type</pre>	Numeric vector. An indicator of length $p$ for which variables should be treated as ranks. (1 for rank and 0 to assume the observed marginal distribution). The default is currently to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
iter	Number of iterations (posterior samples; defaults to 1000).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?

### Details

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

An object of class mvn\_imputation:

• imputed\_datasets An array including the imputed datasets.

#### References

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

### Examples

```
# obs
n <- 5000
# n missing
n_missing <- 1000
# variables
p <- 16
# data
Y <- MASS::mvrnorm(n, rep(0, p), ptsd_cor1)</pre>
# for checking
Ymain <- Y
# all possible indices
indices <- which(matrix(0, n, p) == 0,</pre>
                  arr.ind = TRUE)
# random sample of 1000 missing values
na_indices <- indices[sample(5:nrow(indices),</pre>
                               size = n_missing,
                               replace = FALSE),]
# fill with NA
Y[na_indices] <- NA
\# missing = 1
Y_miss <- ifelse(is.na(Y), 1, 0)</pre>
# true values (to check)
true <- unlist(sapply(1:p, function(x)</pre>
        Ymain[which(Y_miss[,x] == 1),x] ))
# impute
fit_missing <- impute_data(Y, progress = FALSE, iter = 250)</pre>
# impute
fit_missing <- impute_data(Y,</pre>
                             progress = TRUE,
```

iri

## Data: Interpersonal Reactivity Index (IRI)

### Description

A dataset containing items from the Interpersonal Reactivity Index (IRI; an empathy measure). There are 28 variables and 1973 observations

### Usage

data("iri")

### Format

A data frame with 28 variables and 1973 observations (5 point Likert scale)

### Details

- 1 I daydream and fantasize, with some regularity, about things that might happen to me.
- 2 I often have tender, concerned feelings for people less fortunate than me.
- 3 I sometimes find it difficult to see things from the "other guy's" point of view.
- 4 Sometimes I don't feel very sorry for other people when they are having problems.
- 5 I really get involved with the feelings of the characters in a novel.
- 6 In emergency situations, I feel apprehensive and ill-at-ease.
- 7 I am usually objective when I watch a movie or play, and I don't often get completely caught up in it.
- 8 I try to look at everybody's side of a disagreement before I make a decision.
- 9 When I see someone being taken advantage of, I feel kind of protective towards them.
- 10 I sometimes feel helpless when I am in the middle of a very emotional situation.
- 11 I sometimes try to understand my friends better by imagining how things look from their perspective
- 12 Becoming extremely involved in a good book or movie is somewhat rare for me.
- 13 When I see someone get hurt, I tend to remain calm.
- 14 Other people's misfortunes do not usually disturb me a great deal.
- 15 If I'm sure I'm right about something, I don't waste much time listening to other people's arguments.
- 16 After seeing a play or movie, I have felt as though I were one of the characters.
- 17 Being in a tense emotional situation scares me.

- 18 When I see someone being treated unfairly, I sometimes don't feel very much pity for them.
- 19 I am usually pretty effective in dealing with emergencies.
- 20 I am often quite touched by things that I see happen.
- 21 I believe that there are two sides to every question and try to look at them both.
- 22 I would describe myself as a pretty soft-hearted person.
- 23 When I watch a good movie, I can very easily put myself in the place of a leading character
- 24 I tend to lose control during emergencies.
- 25 When I'm upset at someone, I usually try to "put myself in his shoes" for a while.
- 26 When I am reading an interesting story or novel, I imagine how I would feel if the events in the story were happening to me.
- 27 When I see someone who badly needs help in an emergency, I go to pieces.
- 28 Before criticizing somebody, I try to imagine how I would feel if I were in their place.
- gender "M" (male) or "F" (female)

## Note

There are four domains

Fantasy: items 1, 5, 7, 12, 16, 23, 26

Perspective taking: items 3, 8, 11, 15, 21, 25, 28

Empathic concern: items 2, 4, 9, 14, 18, 20, 22

Personal distress: items 6, 10, 13, 17, 19, 24, 27,

#### References

Briganti, G., Kempenaers, C., Braun, S., Fried, E. I., & Linkowski, P. (2018). Network analysis of empathy items from the interpersonal reactivity index in 1973 young adults. Psychiatry research, 265, 87-92.

#### Examples

data("iri")

map

Maximum A Posteriori Precision Matrix

## Description

Maximum A Posteriori Precision Matrix

#### Usage

map(Y)

#### pcor\_mat

#### Arguments

Y

Matrix (or data frame) of dimensions *n* (observations) by *p* (variables).

#### Value

An object of class map, including the precision matrix, partial correlation matrix, and regression parameters.

## Examples

```
Y <- BGGM::bfi[, 1:5]
# map
map <- map(Y)
map</pre>
```

pcor\_mat

Extract the Partial Correlation Matrix

### Description

Extract the partial correlation matrix (posterior mean) from estimate, explore, ggm\_compare\_estimate, and ggm\_compare\_explore objects. It is also possible to extract the partial correlation differences for ggm\_compare\_estimate and ggm\_compare\_explore objects.

## Usage

```
pcor_mat(object, difference = FALSE, ...)
```

## Arguments

object	A model estimated with <b>BGGM</b> . All classes are supported, assuming there is matrix to be extracted.
difference	Logical. Should the difference be returned (defaults to FALSE) ? Note that this assumes there is a difference (e.g., an object of class ggm_compare_estimate) and ignored otherwise.
	Currently ignored.

### Value

The estimated partial correlation matrix.

# Examples

pcor\_sum

### Partial Correlation Sum

## Description

Compute and test partial correlation sums either within or between GGMs (e.g., different groups), resulting in a posterior distribution.

### Usage

pcor\_sum(..., iter = NULL, relations)

## Arguments

• • •	An object of class estimate. This can be either one or two fitted objects.
iter	Number of iterations (posterior samples; defaults to the number in the object)
relations	Character string. Which partial correlations should be summed?

#### Details

Some care must be taken when writing the string for partial\_sum. Below are several examples **Just a Sum**: Perhaps a sum is of interest, and not necessarily the difference of two sums. This can be written as

• partial\_sum <- c("A1--A2 + A1--A3 + A1--A4")

which will sum those relations.

Comparing Sums: When comparing sums, each must be seperated by ";". For example,

• partial\_sum <- c("A1--A2 + A1--A3; A1--A2 + A1--A4")

58

which will sum both and compute the difference. Note that there cannot be more than two sums, such that c("A1-A2 + A1-A3; A1-A2 + A1-A4; A1-A2 + A1-A5") will result in an error.

#### **Comparing Groups:**

When more than one fitted object is suppled to object it is assumed that the groups should be compared for the same sum. Hence, in this case, only the sum needs to be written.

• partial\_sum <- c("A1--A2 + A1--A3 + A1--A4")

The above results in that sum being computed for each group and then compared.

### Value

An object of class posterior\_sum, including the sum and possibly the difference for two sums.

#### Examples

```
# data
Y <- bfi
# males
Y_males <- subset(Y, gender == 1, select = -c(education, gender))[,1:5]</pre>
# females
Y_females <- subset(Y, gender == 2, select = -c(education, gender))[,1:5]</pre>
# males
fit_males <- estimate(Y_males, seed = 1,</pre>
                       progress = FALSE)
# fit females
fit_females <- estimate(Y_females, seed = 2,</pre>
                          progress = FALSE)
sums <- pcor_sum(fit_males,</pre>
                  fit_females,
                  relations = "A1--A2 + A1--A3")
# print
sums
# plot difference
plot(sums)[[3]]
```

```
pcor_to_cor
```

### Description

Convert the partial correlation matrices into correlation matrices. To our knowledge, this is the only Bayesian implementation in R that can estiamte Pearson's, tetrachoric (binary), polychoric (ordinal with more than two cateogries), and rank based correlation coefficients.

#### Usage

pcor\_to\_cor(object, iter = NULL)

### Arguments

object	An object of class estimate or explore
iter	numeric. How many iterations (i.e., posterior samples) should be used ? The default uses all of the samples, but note that this can take a long time with large matrices.

### Value

- R An array including the correlation matrices (of dimensions p by p by *iter*)
- R\_mean Posterior mean of the correlations (of dimensions *p* by *p*)

#### Note

The 'default' prior distributions are specified for partial correlations in particular. This means that the implied prior distribution will not be the same for the correlations.

### Examples

## plot.confirm

```
###### ordinal ########
# first level must be 1 !
Y <- Y + 1
# estimate the model
fit <- estimate(Y, type = "ordinal",</pre>
             iter = 250,
             progress = FALSE)
# compute correlations
cors <- pcor_to_cor(fit)</pre>
####### mixed
               ######
# rank based correlations
# estimate the model
fit <- estimate(Y, type = "mixed",</pre>
             iter = 250,
             progress = FALSE)
# compute correlations
cors <- pcor_to_cor(fit)</pre>
```

plot.confirm *Plot* confirm *objects* 

#### Description

Plot the posterior hypothesis probabilities as a pie chart, with each slice corresponding the probability of a given hypothesis.

#### Usage

## S3 method for class 'confirm'
plot(x, ...)

### Arguments

Х	An object of class confirm
	Currently ignored.

## Value

A ggplot object.

## Examples

```
##### example 1: many relations #####
# data
Y <- bfi
hypothesis <- c("g1_A1--A2 > g2_A1--A2 & g1_A1--A3 = g2_A1--A3;
               g1_A1--A2 = g2_A1--A2 & g1_A1--A3 = g2_A1--A3;
               g1_A1-A2 = g2_A1-A2 = g1_A1-A3 = g2_A1-A3"
     <- subset(Y, gender == 1,
Ymale
                select = -c(education,
                          gender))[,1:5]
# females
Yfemale <- subset(Y, gender == 2,</pre>
                  select = -c(education),
                             gender))[,1:5]
test <- ggm_compare_confirm(Ymale,</pre>
                        Yfemale,
                        hypothesis = hypothesis,
                        iter = 250,
                        progress = FALSE)
# plot
```

plot(test)

plot.ggm\_compare\_ppc Plot ggm\_compare\_ppc Objects

# Description

Plot the predictive check with ggridges

## plot.ggm\_compare\_ppc

## Usage

```
## S3 method for class 'ggm_compare_ppc'
plot(
    x,
    critical = 0.05,
    col_noncritical = "#84e184A0",
    col_critical = "red",
    point_size = 2,
    ...
)
```

## Arguments

х	An object of class ggm_compare_ppc	
critical	Numeric. The 'significance' level (defaults to 0.05).	
col_noncritical		
	Character string. Fill color for the non-critical region (defaults to "#84e184A0").	
col_critical	Character string. Fill color for the critical region (defaults to "red").	
point_size	Numeric. The point size for the observed score (defaults to 2).	
	Currently ignored.	

# Value

An object (or list of objects) of class ggplot.

### Note

See ggridges for many examples.

## See Also

ggm\_compare\_ppc

## Examples

Yf <- subset(Y, gender == 2,</pre>

```
select = - c(gender, education))
```

plot(global\_test)

plot.pcor\_sum Plot pcor\_sum Object

## Description

Plot pcor\_sum Object

# Usage

```
## S3 method for class 'pcor_sum'
plot(x, fill = "#CC79A7", ...)
```

# Arguments

Х	An object of class posterior_sum
fill	Character string. What fill for the histogram (defaults to colorblind "pink")?
	Currently ignored.

## Value

A list of ggplot objects

## Note

Examples:

## See Also

pcor\_sum

# Description

Plot predictability Objects

## Usage

```
## S3 method for class 'predictability'
plot(
    x,
    type = "error_bar",
    cred = 0.95,
    alpha = 0.5,
    scale = 1,
    width = 0,
    size = 1,
    color = "blue",
    ...
)
```

## Arguments

х	An object of class predictability
type	Character string. Which type of plot ? The options are "error_bar" or "ridgeline" (defaults to "error_bar").
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
alpha	Numeric. Transparancey of the ridges
scale	Numeric. This controls the overlap of densities for type = "ridgeline" (de- faults to 1).
width	Numeric. The width of error bar ends (defaults to $0$ ) for type = "error_bar".
size	Numeric. The size for the points (defaults to 2) for type = "error_bar".
color	Character string. What color for the point (type = "error_bar") or tail region (type = "ridgeline")? Defaults to "blue".
	Currently ignored.

## Value

An object of class ggplot.

# Examples

plot.roll\_your\_own Plot roll\_your\_own Objects

## Description

Plot roll\_your\_own Objects

### Usage

## S3 method for class 'roll\_your\_own'
plot(x, fill = "#CC79A7", alpha = 0.5, ...)

### Arguments

Х	An object of class roll_your_own
fill	Character string specifying the color for the ridges.
alpha	Numeric. Transparancey of the ridges
	Currently ignored

## Value

An object of class ggplot

## Examples

membership <- c(rep("a", 5), rep("c", 5))</pre>

66

## plot.select

```
# fit model
fit <- estimate(Y = Y, iter = 250,</pre>
                 progress = FALSE)
# membership
membership <- c(rep("a", 5), rep("c", 5))</pre>
# define function
f \leftarrow function(x,...)
 assortment.discrete(x, ...)$r
}
net_stat <- roll_your_own(object = fit,</pre>
                            FUN = f,
                            types = membership,
                            weighted = TRUE,
                            SE = FALSE, M = 1,
                            progress = FALSE)
# plot
plot(net_stat)
```

plot.select	Network Plot for select Objects
prot.screet	neiwork i loi jor serece objects

## Description

Visualize the conditional (in)dependence structure.

### Usage

```
## S3 method for class 'select'
plot(
    x,
    layout = "circle",
    pos_col = "#009E73",
    neg_col = "#D55E00",
    node_size = 10,
    edge_magnify = 1,
    groups = NULL,
    palette = "Set3",
    ...
)
```

## Arguments

х	An object of class select.
layout	Character string. Which graph layout (defaults is circle)? See gplot.layout.
pos_col	Character string. Color for the positive edges (defaults to green).
neg_col	Character string. Color for the negative edges (defaults to green).
node_size	Numeric. The size of the nodes (defaults to 10).
edge_magnify	Numeric. A value that is multiplied by the edge weights. This increases $(> 1)$ or decrease $(< 1)$ the line widths (defaults to 1).
groups	A character string of length $p$ (the number of nodes in the model). This indicates groups of nodes that should be the same color (e.g., "clusters" or "communities").
palette	A character string sepcifying the palette for the groups. (default is Set3). See palette options here.
	Additional options passed to ggnet2

## Value

An object (or list of objects) of class ggplot that can then be further customized.

#### Note

A more extensive example of a custom plot is provided here

# Examples

```
### example 1: one ggm ##
# data
Y <- bfi[,1:25]
# estimate
fit <- estimate(Y, iter = 250,</pre>
              progress = FALSE)
# "communities"
comm <- substring(colnames(Y), 1, 1)</pre>
# edge set
E <- select(fit)</pre>
# plot edge set
plt_E <- plot(E, edge_magnify = 5,</pre>
             palette = "Set1",
             groups = comm)
```

```
### example 2: ggm compare ##
# compare males vs. females
# data
Y <- bfi[,1:26]
Ym <- subset(Y, gender == 1,</pre>
            select = -gender)
Yf <- subset(Y, gender == 2,</pre>
             select = -gender)
# estimate
fit <- ggm_compare_estimate(Ym, Yf, iter = 250,</pre>
                          progress = FALSE)
# "communities"
comm <- substring(colnames(Ym), 1, 1)</pre>
# edge set
E <- select(fit)</pre>
# plot edge set
plt_E <- plot(E, edge_magnify = 5,</pre>
             palette = "Set1",
             groups = comm)
```

plot.summary.estimate Plot summary.estimate Objects

### Description

Visualize the posterior distributions for each partial correlation.

# Usage

```
## S3 method for class 'summary.estimate'
plot(x, color = "black", size = 2, width = 0, ...)
```

# Arguments

х	An object of class summary.estimate
color	Character string. The color for the error bars. (defaults to "black").

size	Numeric. The size for the points (defaults to 2).
width	Numeric. The width of error bar ends (defaults to $0$ ).
	Currently ignored

# Value

A ggplot object.

### See Also

estimate

## Examples

```
plot(summary(fit))
```

plot.summary.explore Plot summary.explore Objects

## Description

Visualize the posterior distributions for each partial correlation.

## Usage

```
## S3 method for class 'summary.explore'
plot(x, color = "black", size = 2, width = 0, ...)
```

## Arguments

х	An object of class summary.explore
color	Character string. The color for the error bars. (defaults to "black").
size	Numeric. The size for the points (defaults to 2).
width	Numeric. The width of error bar ends (defaults to 0).
•••	Currently ignored

# Value

A ggplot object

## See Also

explore

## Examples

## Description

Visualize the posterior distribution differences.

### Usage

```
## S3 method for class 'summary.ggm_compare_estimate'
plot(x, color = "black", size = 2, width = 0, ...)
```

### Arguments

х	An object of class ggm_compare_estimate.
color	Character string. The color of the points (defaults to "black").
size	Numeric. The size of the points (defaults to 2).
width	Numeric. The width of error bar ends (defaults to 0).
	Currently ignored.

## Value

An object of class ggplot

## See Also

ggm\_compare\_estimate

## Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                 select = -c(gender),
                             education))[,1:5]
Yfemale <- subset(Y, gender == 2,</pre>
                   select = -c(gender,
                               education))[,1:5]
# fit model
fit <- ggm_compare_estimate(Ymale, Yfemale,</pre>
                              type = "ordinal",
                             iter = 250,
                             prior_sd = 0.25,
                              progress = FALSE)
plot(summary(fit))
```

## Description

Visualize the posterior hypothesis probabilities.

### Usage

```
## S3 method for class 'summary.ggm_compare_explore'
plot(x, size = 2, color = "black", ...)
```

## Arguments

Х	An object of class summary.ggm_compare_explore
size	Numeric. The size of the points (defaults to 2).
color	Character string. The color of the points (defaults to "black").
	Currently ignored.

72

## Value

A ggplot object

## See Also

ggm\_compare\_explore

### Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                 select = -c(gender,
                             education))[,1:10]
Yfemale <- subset(Y, gender == 2,</pre>
                   select = -c(gender,
                               education))[,1:10]
### example 1: ordinal ###
# fit model
fit <- ggm_compare_explore(Ymale, Yfemale,</pre>
                         type = "ordinal",
                         iter = 250,
                         progress = FALSE)
# summary
summ <- summary(fit)</pre>
plot(summ)
```

### Description

Visualize the posterior hypothesis probabilities.

#### Usage

```
## S3 method for class 'summary.select.explore'
plot(x, size = 2, color = "black", ...)
```

# Arguments

х	An object of class summary.select.explore	
size	Numeric. The size for the points (defaults to 2).	
color	Character string. The Color for the points	
	Currently ignored	

# Value

A ggplot object

## Examples

plot.summary.var\_estimate

```
Plot summary.var_estimate Objects
```

# Description

Visualize the posterior distributions of each partial correlation and regression coefficient.

### Usage

```
## S3 method for class 'summary.var_estimate'
plot(x, color = "black", size = 2, width = 0, param = "all", order = TRUE, ...)
```

## plot\_prior

### Arguments

х	An object of class summary.var_estimate
color	Character string. The color for the error bars. (defaults to "black").
size	Numeric. The size for the points (defaults to 2).
width	Numeric. The width of error bar ends (defaults to 0).
param	Character string. Which parameters should be plotted ? The options are pcor, beta, or all (default).
order	Logical. Should the relations be ordered by size (defaults to TRUE) ?
	Currently ignored

### Value

A list of ggplot objects.

# Examples

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
plts <- plot(summary(fit))
plts$pcor_plt</pre>
```

plot\_prior

Plot: Prior Distribution

## Description

Visualize the implied prior distribution for the partial correlations. This is particularly useful for the Bayesian hypothesis testing methods.

### Usage

plot\_prior(prior\_sd = 0.2, iter = 5000)

## Arguments

prior_sd	Scale of the prior distribution, approximately the standard deviation of a beta
	distribution (defaults to 0.25).
iter	Number of iterations (prior samples; defaults to 5000).

### Value

A ggplot object.

## Examples

# note: iter = 250 for demonstrative purposes

plot\_prior(prior\_sd = 0.25, iter = 250)

posterior\_predict Posterior Predictive Distribution

### Description

Draw samples from the posterior predictive distribution.

#### Usage

```
posterior_predict(object, iter = 1000, progress = TRUE)
```

### Arguments

object	An object of class estimate or explore
iter	Numeric. Number of samples from the predictive distribution
progress	Logical. Should a progress bar be included (defaults to TRUE)

#### Value

A 3D array containing the predicted datasets

# Note

Currently only implemented for type = "mixed", type = "ordinal", and type = "binary". Note the term mixed is confusing, in that it can be used with only, say, ordinal data. In this case, reestimate the model with type = "mixed" until all data types are supported.

## Examples

76

### Description

Extract posterior samples for all parameters.

### Usage

```
posterior_samples(object, ...)
```

### Arguments

object	an object of class estimate or explore.
	currently ignored.

# Value

A matrix of posterior samples for the partial correlation. Note that if controlling for variables (e.g., formula ~ age), the matrix also includes the coefficients from each multivariate regression.

```
# note: iter = 250 for demonstrative purposes
****
### example 1: control with formula ###
# (the following works with all data types)
# controlling for gender
Y <- bfi
# to control for only gender
# (remove education)
Y <- subset(Y, select = - education)</pre>
# fit model
fit <- estimate(Y, formula = ~ gender,</pre>
              iter = 250)
# note regression coefficients
samps <- posterior_samples(fit)</pre>
hist(samps[,1])
```

precision

## Description

Transform the sampled correlation matrices to precision matrices (i.e., inverse covariance matrices).

#### Usage

```
precision(object, progress = TRUE)
```

## Arguments

object	An object of class estimate.
progress	Logical. Should a progress bar be included (defaults to TRUE)?

## Value

- precision\_mean The mean of the precision matrix (p by p matrix).
- precision 3d array of dimensions p by p by iter including **unconstrained** (i.e., from th full graph) precision matrices.

### Note

The estimated precision matrix is the inverse of the correlation matrix.

```
# data
Y <- ptsd
# fit model
fit <- estimate(Y)
# precision matrix
Theta <- precision(fit)</pre>
```

predict.estimate Model Predictions for estimate Objects

### Description

Model Predictions for estimate Objects

### Usage

```
## S3 method for class 'estimate'
predict(
   object,
   newdata = NULL,
   summary = TRUE,
   cred = 0.95,
   iter = NULL,
   progress = TRUE,
   ...
)
```

## Arguments

object	object of class estimate
newdata	an optional data frame for obtaining predictions (e.g., on test data)
summary	summarize the posterior samples (defaults to TRUE).
cred	credible interval used for summarizing
iter	number of posterior samples (defaults to all in the object).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
	currently ignored

### Value

summary = TRUE: 3D array of dimensions n (observations), 4 (posterior summary), p (number of nodes). summary = FALSE: list containing predictions for each variable

predict.explore

## Description

Model Predictions for explore Objects

# Usage

```
## S3 method for class 'explore'
predict(
   object,
   newdata = NULL,
   summary = TRUE,
   cred = 0.95,
   iter = NULL,
   progress = TRUE,
   ...
)
```

## Arguments

object	object of class explore
newdata	an optional data frame for obtaining predictions (e.g., on test data)
summary	summarize the posterior samples (defaults to TRUE).
cred	credible interval used for summarizing
iter	number of posterior samples (defaults to all in the object).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
	currently ignored

# Value

summary = TRUE: 3D array of dimensions n (observations), 4 (posterior summary), p (number of nodes). summary = FALSE: list containing predictions for each variable

## Examples

# predict

predict.var\_estimate Model Predictions for var\_estimate Objects

### Description

Model Predictions for var\_estimate Objects

# Usage

```
## S3 method for class 'var_estimate'
predict(object, summary = TRUE, cred = 0.95, iter = NULL, progress = TRUE, ...)
```

# Arguments

object	object of class var_estimate
summary	summarize the posterior samples (defaults to TRUE).
cred	credible interval used for summarizing
iter	number of posterior samples (defaults to all in the object).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
	Currently ignored

#### Value

The predicted values for each regression model.

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
# fitted values
pred <- predict(fit, progress = FALSE)
# predicted values (1st outcome)
pred[,,1]</pre>
```

predictability

# Description

Compute nodewise predictability or Bayesian variance explained (R2 Gelman et al. 2019). In the context of GGMs, this method was described in Williams (2018).

#### Usage

```
predictability(
   object,
   select = FALSE,
   cred = 0.95,
   BF_cut = 3,
   iter = NULL,
   progress = TRUE,
   ...
)
```

## Arguments

object	object of class estimate or explore
select	logical. Should the graph be selected ? The default is currently FALSE.
cred	numeric. credible interval between 0 and 1 (default is 0.95) that is used for selecting the graph.
BF_cut	numeric. evidentiary threshold (default is 3).
iter	interger. iterations (posterior samples) used for computing R2.
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
	currently ignored.

## Value

An object of classes bayes\_R2 and metric, including

• scores A list containing the posterior samples of R2. The is one element for each node.

### Note

## **Binary and Ordinal Data:**

R2 is computed from the latent data.

Mixed Data:

#### predicted\_probability

The mixed data approach is somewhat ad-hoc see for example p. 277 in Hoff (2007). This is becaue uncertainty in the ranks is not incorporated, which means that variance explained is computed from the 'empirical' *CDF*.

### Model Selection:

Currently the default to include all nodes in the model when computing R2. This can be changed (i.e., select = TRUE), which then sets those edges not detected to zero. This is accomplished by subsetting the correlation matrix according to each neighborhood of relations.

## References

Gelman A, Goodrich B, Gabry J, Vehtari A (2019). "R-squared for Bayesian Regression Models." *American Statistician*, **73**(3), 307–309. ISSN 15372731, doi:10.1080/00031305.2018.1549100.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi:10.1214/07AOAS107.

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi:10.31234/OSF.IO/X8DPR.

### Examples

predicted\_probability Predicted Probabilities

### Description

Compute the predicted probabilities for discrete data, with the possibility of conditional predictive probabilities (i.e., at fixed values of other nodes)

#### Usage

```
predicted_probability(object, outcome, Y, ...)
```

#### Arguments

object	An object of class posterior_predict
outcome	Character string. Node for which the probabilities are computed.
Y	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables). This must include the column names.
	Compute conditional probabilities by specifying a column name in Y (besides the outcome) and a fixed value. This can include any number of nodes. See example below. Leave this blank to compute unconditional probabilities for outcome.

### Value

A list containing a matrix with the computed probabilities (a row for each predictive sample and a column for each category).

### Note

There are no checks that the conditional probability exists, i.e., suppose you wish to condition on, say, B3 = 2 and B4 = 1, yet there is no instance in which B3 is 2 AND B4 is 1. This will result in an uninformative error.

## Examples

print.BGGM

Print method for BGGM objects

## Description

Mainly used to avoid a plethora of different print functions that overcrowded the documentation in previous versions of **BGGM**.

#### prior\_belief\_ggm

#### Usage

## S3 method for class 'BGGM'
print(x, ...)

# Arguments

Х	An object of class BGGM
	currently ignored

prior\_belief\_ggm Prior Belief Gaussian Graphical Model

## Description

Incorporate prior information into the estimation of the conditional dependence structure. This prior information is expressed as the prior odds that each relation should be included in the graph.

#### Usage

```
prior_belief_ggm(Y, prior_ggm, post_odds_cut = 3, ...)
```

## Arguments

Υ	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables/nodes).
prior_ggm	Matrix of dimensions $p$ by $p$ , encoding the prior odds for including each relation in the graph (see 'Details')
post_odds_cut	Numeric. Threshold for including an edge (defaults to 3). Note post_odds refers to posterior odds.
	Additional arguments passed to explore.

#### Details

Technically, the prior odds is not for including an edge in the graph, but for (H1)/p(H0), where H1 captures the hypothesized edge size and H0 is the null model (see Williams2019\_bf). Accordingly, setting an entry in prior\_ggm to, say, 10, encodes a prior belief that H1 is 10 times more likely than H0. Further, setting an entry in prior\_ggm to 1 results in equal prior odds (the default in select.explore).

#### Value

An object including:

- adj: Adjacency matrix
- post\_prob: Posterior probability for the alternative hypothesis.

# Examples

```
# Assume perfect prior information
# synthetic ggm
p <- 20
main <- gen_net()</pre>
# prior odds 10:1, assuming graph is known
prior_ggm <- ifelse(main$adj == 1, 10, 1)</pre>
# generate data
y \leq MASS::mvrnorm(n = 200,
                   mu = rep(0, 20),
                    Sigma = main$cors)
# prior est
prior_est <- prior_belief_ggm(Y = y,</pre>
                               prior_ggm = prior_ggm,
                               progress = FALSE)
# check scores
BGGM:::performance(Estimate = prior_est$adj,
                    True = main$adj)
# default in BGGM
default_est <- select(explore(y, progress = FALSE))</pre>
# check scores
BGGM:::performance(Estimate = default_est$Adj_10,
                   True = main$adj)
```

prior\_belief\_var Prior Belief Graphical VAR

### Description

Prior Belief Graphical VAR

### Usage

```
prior_belief_var(
    Y,
    prior_temporal = NULL,
    post_odds_cut = 3,
    est_ggm = TRUE,
    prior_ggm = NULL,
    progress = TRUE,
```

86

) ...

### Arguments

Υ	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables/nodes).
prior_temporal	Matrix of dimensions $p$ by $p$ , encoding the prior odds for including each relation in the temporal graph (see 'Details'). If null a matrix of 1's is used, resulting in equal prior odds.
post_odds_cut	Numeric. Threshold for including an edge (defaults to 3). Note post_odds refers to posterior odds.
est_ggm	Logical. Should the contemporaneous network be estimated (defaults to TRUE)?
prior_ggm	Matrix of dimensions $p$ by $p$ , encoding the prior odds for including each relation in the graph (see 'Details'). If null a matrix of 1's is used, resulting in equal prior odds.
progress	Logical. Should a progress bar be included (defaults to TRUE)?
	Additional arguments passed to explore. Ignored if prior_ggm = FALSE.

### Details

Technically, the prior odds is not for including an edge in the graph, but for (H1)/p(H0), where H1 captures the hypothesized edge size and H0 is the null model (see Williams2019\_bf). Accordingly, setting an entry in prior\_ggm to, say, 10, encodes a prior belief that H1 is 10 times more likely than H0. Further, setting an entry in prior\_ggm or prior\_var to 1 results in equal prior odds (the default in select.explore).

#### Value

An object including (est\_ggm = FALSE):

- **adj**: Adjacency matrix
- post\_prob: Posterior probability for the alternative hypothesis.

An object including (est\_ggm = TRUE):

- adj\_temporal: Adjacency matrix for the temporal network.
- post\_prob\_temporal: Posterior probability for the alternative hypothesis (temporal edge)
- adj\_ggm: Adjacency matrix for the contemporaneous network (ggm).
- post\_prob\_ggm: Posterior probability for the alternative hypothesis (contemporaneous edge)

#### Note

The returned matrices are formatted with the rows indicating the outcome and the columns the predictor. Hence, adj\_temporal[1,4] is the temporal relation of node 4 predicting node 1. This follows the convention of the **vars** package (i.e., Acoef).

Further, in order to compute the Bayes factor the data is standardized (mean = 0 and standard deviation = 1).

# Examples

```
ptsd
```

Data: Post-Traumatic Stress Disorder

## Description

A dataset containing items that measure Post-traumatic stress disorder symptoms (Armour et al. 2017). There are 20 variables (p) and 221 observations (n).

## Usage

data("ptsd")

### Format

A dataframe with 221 rows and 20 variables

### Details

- Intrusive Thoughts
- Nightmares
- Flashbacks
- Emotional cue reactivity
- Psychological cue reactivity
- Avoidance of thoughts
- Avoidance of reminders
- Trauma-related amnesia
- Negative beliefs

#### 88

## ptsd\_cor1

- · Negative trauma-related emotions
- Loss of interest
- Detachment
- Restricted affect
- Irritability/anger
- · Self-destructive/reckless behavior
- Hypervigilance
- Exaggerated startle response
- Difficulty concentrating
- Sleep disturbance

#### References

Armour C, Fried EI, Deserno MK, Tsai J, Pietrzak RH (2017). "A network analysis of DSM-5 posttraumatic stress disorder symptoms and correlates in US military veterans." *Journal of anxiety disorders*, **45**, 49–59. doi:10.31234/osf.io/p69m7.

ptsd\_cor1

Data: Post-Traumatic Stress Disorder (Sample # 1)

#### Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 526 individuals (Fried et al. 2018).

### Format

A correlation matrix with 16 variables

#### Details

- Intrusive Thoughts
- Nightmares
- Flashbacks
- Physiological/psychological reactivity
- Avoidance of thoughts
- Avoidance of situations
- Amnesia
- Disinterest in activities
- · Feeling detached
- Emotional numbing
- Foreshortened future

- Sleep problems
- Irritability
- Concentration problems
- Hypervigilance
- Startle response

#### References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

### Examples

```
data(ptsd_cor1)
```

```
Y <- MASS::mvrnorm(n = 526,
    mu = rep(0, 16),
    Sigma = ptsd_cor1,
    empirical = TRUE)
```

ptsd\_cor2

```
Data: Post-Traumatic Stress Disorder (Sample # 2)
```

### Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 365 individuals (Fried et al. 2018).

## Format

A correlation matrix with 16 variables

#### Details

- Intrusive Thoughts
- Nightmares
- Flashbacks
- Physiological/psychological reactivity
- Avoidance of thoughts
- · Avoidance of situations
- Amnesia

## ptsd\_cor3

- Disinterest in activities
- · Feeling detached
- Emotional numbing
- Foreshortened future
- · Sleep problems
- Irritability
- Concentration problems
- Hypervigilance
- Startle response

## References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

## Examples

ptsd\_cor3

Data: Post-Traumatic Stress Disorder (Sample # 3)

### Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 926 individuals (Fried et al. 2018).

### Format

A correlation matrix with 16 variables

#### Details

- Intrusive Thoughts
- Nightmares
- Flashbacks
- · Physiological/psychological reactivity
- Avoidance of thoughts

- Avoidance of situations
- Amnesia
- Disinterest in activities
- · Feeling detached
- Emotional numbing
- · Foreshortened future
- · Sleep problems
- Irritability
- Concentration problems
- Hypervigilance
- · Startle response

#### References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

### Examples

ptsd\_cor4

Data: Post-Traumatic Stress Disorder (Sample # 4)

### Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 965 individuals (Fried et al. 2018).

## Format

A correlation matrix with 16 variables

### Details

- Intrusive Thoughts
- Nightmares
- Flashbacks
- Physiological/psychological reactivity
- Avoidance of thoughts
- Avoidance of situations
- Amnesia
- Disinterest in activities
- · Feeling detached
- · Emotional numbing
- Foreshortened future
- Sleep problems
- Irritability
- Concentration problems
- Hypervigilance
- Startle response

### References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

#### Examples

regression\_summary Summarary Method for Multivariate or Univarate Regression

### Description

Summarary Method for Multivariate or Univarate Regression

## Usage

```
regression_summary(object, cred = 0.95, ...)
```

### Arguments

object	An object of class estimate
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
	Currently ignored

# Value

A list of length *p* including the summaries for each regression.

# Examples

roll\_your\_own Compute Custom Network Statistics

# Description

This function allows for computing custom network statistics for weighted adjacency matrices (partial correlations). The statistics are computed for each of the sampled matrices, resulting in a distribution.

#### Usage

```
roll_your_own(
   object,
   FUN,
   iter = NULL,
   select = FALSE,
   cred = 0.95,
   progress = TRUE,
```

) ...

### Arguments

object	An object of class estimate.
FUN	A custom function for computing the statistic. The first argument must be a partial correlation matrix.
iter	Number of iterations (posterior samples; defaults to the number in the object).
select	Logical. Should the graph be selected ? The default is currently FALSE.
cred	Numeric. Credible interval between 0 and 1 (default is 0.95) that is used for selecting the graph.
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
	Arguments passed to the function.

## Details

The user has complete control of this function. Hence, care must be taken as to what FUN returns and in what format. The function should return a single number (one for the entire GGM) or a vector (one for each node). This ensures that the print and plot.roll\_your\_own will work.

When select = TRUE, the graph is selected and then the network statistics are computed based on the weighted adjacency matrix. This is accomplished internally by multiplying each of the sampled partial correlation matrices by the adjacency matrix.

#### Value

An object defined by FUN.

```
}
net_stat <- roll_your_own(object = fit,</pre>
                      FUN = f,
                      types = membership,
                      weighted = TRUE,
                      SE = FALSE, M = 1,
                      progress = FALSE)
# print
net_stat
###### example 2: expected influence #######
*****
# expected influence from this package
library(networktools)
# data
Y <- depression
# fit model
fit <- estimate(Y = Y, iter = 250)</pre>
# define function
f \leftarrow function(x,...)
    expectedInf(x,...)$step1
}
# compute
net_stat <- roll_your_own(object = fit,</pre>
                      FUN = f,
                      progress = FALSE)
### example 3: mixed data & bridge ####
****
# bridge from this package
library(networktools)
# data
Y <- ptsd[,1:7]
fit <- estimate(Y,</pre>
              type = "mixed",
              iter = 250)
# clusters
communities <- substring(colnames(Y), 1, 1)</pre>
```

assortment.discrete(x, ...)\$r

96

97

```
# function is slow
f <- function(x, ...){
bridge(x, ...)$`Bridge Strength`
}
net_stat <- roll_your_own(fit,
FUN = f,
select = TRUE,
communities = communities,
progress = FALSE)
```

rsa

Data: Resilience Scale of Adults (RSA)

## Description

A dataset containing items from the Resilience Scale of Adults (RSA). There are 33 items and 675 observations

## Usage

data("rsa")

### Format

A data frame with 28 variables and 1973 observations (5 point Likert scale)

#### Details

- 1 My plans for the future are
- 2 When something unforeseen happens
- 3 My family understanding of what is important in life is
- 4 I feel that my future looks
- 5 My goals
- 6 I can discuss personal issues with
- 7 I feel
- 8 I enjoy being
- 9 Those who are good at encouraging are
- 10 The bonds among my friends
- 11 My personal problems
- 12 When a family member experiences a crisis/emergency
- 13 My family is characterised by

rsa

- 14 To be flexible in social settings
- 15 I get support from
- 16 In difficult periods my family
- 17 My judgements and decisions
- 18 New friendships are something
- 19 When needed, I have
- 20 I am at my best when I
- 21 Meeting new people is
- 22 When I am with others
- 23 When I start on new things/projects
- 24 Facing other people, our family acts
- 25 Belief in myself
- 26 For me, thinking of good topics of conversation is
- 27 My close friends/family members
- 28 I am good at
- 29 In my family, we like to
- 30 Rules and regular routines
- 31 In difficult periods I have a tendency to
- 32 My goals for the future are
- 33 Events in my life that I cannot influence
- gender "M" (male) or "F" (female)

## Note

There are 6 domains

Planned future: items 1, 4, 5, 32

Perception of self: items 2, 11, 17, 25, 31, 33

Family cohesion: items 3, 7, 13, 16, 24, 29

Social resources: items 6, 9, 10, 12, 15, 19, 27

Social Competence: items 8, 14, 18, 21, 22, 26,

Structured style: items 23, 28, 30

## References

Briganti, G., & Linkowski, P. (2019). Item and domain network structures of the Resilience Scale for Adults in 675 university students. Epidemiology and psychiatric sciences, 1-9.

#### Examples

data("rsa")

Sachs

# Description

Protein expression in human immune system cells

## Usage

data("Sachs")

# Format

A data frame containing 7466 cells (n = 7466) and flow cytometry measurements of 11 (p = 11) phosphorylated proteins and phospholipids

@references Sachs, K., Gifford, D., Jaakkola, T., Sorger, P., & Lauffenburger, D. A. (2002). Bayesian network approach to cell signaling pathway modeling. Sci. STKE, 2002(148), pe38-pe38.

## Examples

data("Sachs")

select

S3 select method

# Description

S3 select method

### Usage

select(object, ...)

#### Arguments

object	object of class estimate or explore
	not currently used

#### Value

select works with the following methods:

- select.estimate
- select.explore
- select.ggm\_compare\_estimate

select.estimate

#### Description

Provides the selected graph based on credible intervals for the partial correlations that did not contain zero (Williams 2018).

### Usage

```
## S3 method for class 'estimate'
select(object, cred = 0.95, alternative = "two.sided", ...)
```

### Arguments

object	An object of class estimate.default.
cred	Numeric. The credible interval width for selecting the graph (defaults to 0.95; must be between 0 and 1).
alternative	A character string specifying the alternative hypothesis. It must be one of "two.sided" (default), "greater" or "less". See note for futher details.
	Currently ignored.

### Details

This package was built for the social-behavioral sciences in particular. In these applications, there is strong theory that expects *all* effects to be positive. This is known as a "positive manifold" and this notion has a rich tradition in psychometrics. Hence, this can be incorporated into the graph with alternative = "greater". This results in the estimated structure including only positive edges.

#### Value

The returned object of class select.estimate contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- pcor\_adj Selected partial correlation matrix (weighted adjacency).
- · adj Adjacency matrix for the selected edges
- object An object of class estimate (the fitted model).

# References

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi:10.31234/OSF.IO/X8DPR.

### See Also

estimate and ggm\_compare\_estimate for several examples.

## select.explore

# Examples

select.explore Graph selection for explore Objects

## Description

Provides the selected graph based on the Bayes factor (Williams and Mulder 2019).

### Usage

```
## S3 method for class 'explore'
select(object, BF_cut = 3, alternative = "two.sided", ...)
```

## Arguments

object	An object of class explore.default
BF_cut	Numeric. Threshold for including an edge (defaults to 3).
alternative	A character string specifying the alternative hypothesis. It must be one of "two.sided" (default), "greater", "less", or "exhaustive". See note for further details.
	Currently ignored.

### Details

Exhaustive provides the posterior hypothesis probabilities for a positive, negative, or null relation (see Table 3 in Williams and Mulder 2019).

#### Value

The returned object of class select.explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

alternative = "two.sided"

- pcor\_mat\_zero Selected partial correlation matrix (weighted adjacency).
- pcor\_mat Partial correlation matrix (posterior mean).
- Adj\_10 Adjacency matrix for the selected edges.
- Adj\_01 Adjacency matrix for which there was evidence for the null hypothesis.

alternative = "greater" and "less"

- pcor\_mat\_zero Selected partial correlation matrix (weighted adjacency).
- pcor\_mat Partial correlation matrix (posterior mean).
- Adj\_20 Adjacency matrix for the selected edges.
- Adj\_02 Adjacency matrix for which there was evidence for the null hypothesis (see note).

alternative = "exhaustive"

- post\_prob A data frame that included the posterior hypothesis probabilities.
- neg\_mat Adjacency matrix for which there was evidence for negative edges.
- pos\_mat Adjacency matrix for which there was evidence for positive edges.
- neg\_mat Adjacency matrix for which there was evidence for the null hypothesis (see note).
- pcor\_mat Partial correlation matrix (posterior mean). The weighted adjacency matrices can be computed by multiplying pcor\_mat with an adjacency matrix.

### Note

Care must be taken with the options alternative = "less" and alternative = "greater". This is because the full parameter space is not included, such, for alternative = "greater", there can be evidence for the "null" when the relation is negative. This inference is correct: the null model better predicted the data than the positive model. But note this is relative and does **not** provide absolute evidence for the null hypothesis.

### References

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi:10.31234/osf.io/ypxd8.

#### See Also

explore and ggm\_compare\_explore for several examples.

### Examples

select.ggm\_compare\_estimate

Graph Selection for ggm\_compare\_estimate Objects

#### Description

Provides the selected graph (of differences) based on credible intervals for the partial correlations that did not contain zero (Williams 2018).

### Usage

## S3 method for class 'ggm\_compare\_estimate'
select(object, cred = 0.95, ...)

### Arguments

object	An object of class estimate.default.
cred	Numeric. The credible interval width for selecting the graph (defaults to 0.95; must be between 0 and 1).
	not currently used

### Value

The returned object of class select.ggm\_compare\_estimate contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- mean\_diff A list of matrices for each group comparsion (partial correlation differences).
- pcor\_adj A list of weighted adjacency matrices for each group comparsion.
- adj A list of adjacency matrices for each group comparsion.

# Examples

```
# note: iter = 250 for demonstrative purposes
### example 1: ###
#####################
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
               select = -c(gender,
                           education))
Yfemale <- subset(Y, gender == 2,</pre>
                  select = -c(gender),
                              education))
# fit model
fit <- ggm_compare_estimate(Ymale, Yfemale,</pre>
                           type = "continuous",
                           iter = 250,
                           progress = FALSE)
```

```
E <- select(fit)</pre>
```

# Description

Provides the selected graph (of differences) based on the Bayes factor (Williams et al. 2020).

#### Usage

```
## S3 method for class 'ggm_compare_explore'
select(object, BF_cut = 3, ...)
```

### Arguments

object	An object of class ggm_compare_explore.
BF_cut	Numeric. Threshold for including an edge (defaults to 3).
• • •	Currently ignored.

# 104

#### Value

The returned object of class select.ggm\_compare\_explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- adj\_10 Adjacency matrix for which there was evidence for a difference.
- adj\_10 Adjacency matrix for which there was evidence for a null relation
- pcor\_mat\_10 Selected partial correlation matrix (weighted adjacency; only for two groups).

# See Also

explore and ggm\_compare\_explore for several examples.

## Examples

```
### example 1: ###
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                  select = -c(gender,
                              education))[,1:10]
Yfemale <- subset(Y, gender == 2,</pre>
                    select = -c(gender),
                               education))[,1:10]
# fit model
fit <- ggm_compare_explore(Ymale, Yfemale,</pre>
                          iter = 250,
                          type = "continuous",
                          progress = FALSE)
```

E <- select(fit, post\_prob = 0.50)</pre>

select.var\_estimate Graph Selection for var.estimate Object

### Description

Graph Selection for var.estimate Object

#### Usage

```
## S3 method for class 'var_estimate'
select(object, cred = 0.95, alternative = "two.sided", ...)
```

## Arguments

object	An object of class VAR.estimate.
cred	Numeric. The credible interval width for selecting the graph (defaults to 0.95; must be between 0 and 1).
alternative	A character string specifying the alternative hypothesis. It must be one of "two.sided" (default), "greater" or "less". See note for futher details.
	Currently ignored.

## Value

An object of class select.var\_estimate, including

- pcor\_adj Adjacency matrix for the partial correlations.
- beta\_adj Adjacency matrix for the regression coefficients.
- pcor\_weighted\_adj Weighted adjacency matrix for the partial correlations.
- beta\_weighted\_adj Weighted adjacency matrix for the regression coefficients.
- pcor\_mu Partial correlation matrix (posterior mean).
- beta\_mu A matrix including the regression coefficients (posterior mean).

# Examples

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
# select graphs
select(fit, cred = 0.95)</pre>
```

106

summary.coef

## Description

Summarize regression parameters with the posterior mean, standard deviation, and credible interval.

#### Usage

```
## S3 method for class 'coef'
summary(object, cred = 0.95, ...)
```

### Arguments

object	An object of class coef.
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
	Currently ignored

## Value

A list of length *p* including the summaries for each multiple regression.

#### Note

See coef.estimate and coef.explore for examples.

summary.estimate Summary method for estimate.default objects

## Description

Summarize the posterior distribution of each partial correlation with the posterior mean and standard deviation.

### Usage

```
## S3 method for class 'estimate'
summary(object, col_names = TRUE, cred = 0.95, ...)
```

## Arguments

object	An object of class estimate
col_names	Logical. Should the summary include the column names (default is TRUE)? Setting to FALSE includes the column numbers (e.g., 12).
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
	Currently ignored.

# Value

A dataframe containing the summarized posterior distributions.

# See Also

estimate

# Examples

summary.explore	Summary Method for exp	plore.default Objects
-----------------	------------------------	-----------------------

## Description

Summarize the posterior distribution for each partial correlation with the posterior mean and standard deviation.

# Usage

```
## S3 method for class 'explore'
summary(object, col_names = TRUE, ...)
```

# Arguments

object	An object of class estimate
col_names	Logical. Should the summary include the column names (default is TRUE)? Setting to FALSE includes the column numbers (e.g., 12).
	Currently ignored

A dataframe containing the summarized posterior distributions.

#### See Also

select.explore

#### Examples

summary.ggm\_compare\_estimate

Summary method for ggm\_compare\_estimate objects

# Description

Summarize the posterior distribution of each partial correlation difference with the posterior mean and standard deviation.

## Usage

```
## S3 method for class 'ggm_compare_estimate'
summary(object, col_names = TRUE, cred = 0.95, ...)
```

# Arguments

object	An object of class ggm_compare_estimate.
col_names	Logical. Should the summary include the column names (default is TRUE)? Setting to FALSE includes the column numbers (e.g., 12).
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
	Currently ignored.

## Value

A list containing the summarized posterior distributions.

## See Also

ggm\_compare\_estimate

# Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                 select = -c(gender),
                             education))[,1:5]
Yfemale <- subset(Y, gender == 2,</pre>
                   select = -c(gender,
                               education))[,1:5]
# fit model
fit <- ggm_compare_estimate(Ymale, Yfemale,</pre>
                             type = "ordinal",
                             iter = 250,
                              prior_sd = 0.25,
                              progress = FALSE)
summary(fit)
```

```
summary.ggm_compare_explore
```

Summary Method for ggm\_compare\_explore Objects

# Description

Summarize the posterior hypothesis probabilities

# Usage

```
## S3 method for class 'ggm_compare_explore'
summary(object, col_names = TRUE, ...)
```

# Arguments

object	An object of class ggm_compare_explore.
col_names	Logical. Should the summary include the column names (default is TRUE)? Setting to FALSE includes the column numbers (e.g., 12).
	Currently ignored.

110

An object of class summary.ggm\_compare\_explore

# See Also

ggm\_compare\_explore

## Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                 select = -c(gender,
                             education))[,1:10]
Yfemale <- subset(Y, gender == 2,</pre>
                   select = -c(gender,
                               education))[,1:10]
### example 1: ordinal ###
# fit model
fit <- ggm_compare_explore(Ymale, Yfemale,</pre>
                         type = "ordinal",
                         iter = 250,
                         progress = FALSE)
# summary
summ <- summary(fit)</pre>
summ
```

summary.predictability

Summary Method for predictability Objects

## Description

Summary Method for predictability Objects

# Usage

```
## S3 method for class 'predictability'
summary(object, cred = 0.95, ...)
```

# Arguments

object	An object of class predictability.
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
	Currently ignored

# Examples

 $\verb|summary.select.explore||$ 

Summary Method for select.explore Objects

# Description

Summary Method for select.explore Objects

#### Usage

```
## S3 method for class 'select.explore'
summary(object, col_names = TRUE, ...)
```

## Arguments

object	object of class select.explore.
col_names	Logical.
	Currently ignored.

# 112

a data frame including the posterior mean, standard deviation, and posterior hypothesis probabilities for each relation.

## Examples

summary.var\_estimate Summary Method for var\_estimate Objects

#### Description

Summarize the posterior distribution of each partial correlation and regression coefficient with the posterior mean, standard deviation, and credible intervals.

#### Usage

```
## S3 method for class 'var_estimate'
summary(object, cred = 0.95, ...)
```

# Arguments

object	An object of class var_estimate
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
	Currently ignored.

## Value

A dataframe containing the summarized posterior distributions, including both the partial correlations and the regression coefficients.

- pcor\_results A data frame including the summarized partial correlations
- beta\_results A list containing the summarized regression coefficients (one data frame for each outcome)

## 114

## See Also

var\_estimate

#### Examples

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
# summary ('pcor')
print(
summary(fit, cred = 0.95),
param = "pcor",
)
# summary('beta')
print(
summary(fit, cred = 0.95),
param = "beta",
)
```

tas

#### Data: Toronto Alexithymia Scale (TAS)

## Description

A dataset containing items from the Toronto Alexithymia Scale (TAS). There are 20 variables and 1925 observations

#### Usage

data("tas")

#### Format

A data frame with 20 variables and 1925 observations (5 point Likert scale)

# Details

- 1 I am often confused about what emotion I am feeling
- 2 It is difficult for me to find the right words for my feelings
- 3 I have physical sensations that even doctors don't understand

- 4 I am able to describe my feelings easily
- 5 I prefer to analyze problems rather than just describe them
- 6 When I am upset, I don't know if I am sad, frightened, or angry
- 7 I am often puzzled by sensations in my body
- 8 I prefer just to let things happen rather than to understand why they turned out that way
- 9 I have feelings that I can't quite identify
- 10 Being in touch with emotions is essential
- 11 I find it hard to describe how I feel about people
- 12 People tell me to describe my feelings more
- 13 I don't know what's going on inside me
- 14 I often don't know why I am angry
- 15 I prefer talking to people about their daily activities rather than their feelings
- 16 I prefer to watch "light" entertainment shows rather than psychological dramas
- 17 It is difficult for me to reveal my innermost feelings, even to close friends
- 18 I can feel close to someone, even in moments of silence
- 19 I find examination of my feelings useful in solving personal problems
- · 20 Looking for hidden meanings in movies or plays distracts from their enjoyment
- gender "M" (male) or "F" (female)

## Note

There are three domains

Difficulty identifying feelings: items 1, 3, 6, 7, 9, 13, 14

Difficulty describing feelings: items 2, 4, 11, 12, 17

Externally oriented thinking: items 10, 15, 16, 18, 19

## References

Briganti, G., & Linkowski, P. (2019). Network approach to items and domains from the Toronto Alexithymia Scale. Psychological reports.

#### Examples

data("tas")

var\_estimate

# Description

Estimate VAR(1) models by efficiently sampling from the posterior distribution. This provides two graphical structures: (1) a network of undirected relations (the GGM, controlling for the lagged predictors) and (2) a network of directed relations (the lagged coefficients). Note that in the graphical modeling literature, this model is also known as a time series chain graphical model (Abegaz and Wit 2013).

## Usage

```
var_estimate(
    Y,
    rho_sd = 0.5,
    beta_sd = 1,
    iter = 5000,
    progress = TRUE,
    seed = 1,
    ...
)
```

#### Arguments

Υ	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables).
rho_sd	Numeric. Scale of the prior distribution for the partial correlations, approximately the standard deviation of a beta distribution (defaults to 0.50).
beta_sd	Numeric. Standard deviation of the prior distribution for the regression coefficients (defaults to 1). The prior is by default centered at zero and follows a normal distribution (Equation 9, Sinay and Hsu 2014)
iter	Number of iterations (posterior samples; defaults to 5000).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
seed	An integer for the random seed (defaults to 1).
	Currently ignored.

# Details

Each time series in Y is standardized (mean = 0; standard deviation = 1).

#### Value

An object of class var\_estimate containing a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

• beta\_mu A matrix including the regression coefficients (posterior mean).

- pcor\_mu Partial correlation matrix (posterior mean).
- fit A list including the posterior samples.

# Note

## **Regularization**:

A Bayesian ridge regression can be fitted by decreasing  $beta_sd$  (e.g.,  $beta_sd = 0.25$ ). This could be advantageous for forecasting (out-of-sample prediction) in particular.

# References

Abegaz F, Wit E (2013). "Sparse time series chain graphical models for reconstructing genetic networks." *Biostatistics*, **14**(3), 586–599. doi:10.1093/biostatistics/kxt005.

Sinay MS, Hsu JS (2014). "Bayesian inference of a multivariate regression model." *Journal of Probability and Statistics*, 2014.

#### Examples

```
# data
Y <- subset(ifit, id == 1)[,-1]
# use alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
fit</pre>
```

weighted\_adj\_mat Extract the Weighted Adjacency Matrix

#### Description

Extract the weighted adjacency matrix (posterior mean) from estimate, explore, ggm\_compare\_estimate, and ggm\_compare\_explore objects.

#### Usage

```
weighted_adj_mat(object, ...)
```

#### Arguments

object	A model estimated with BGGM. All classes are supported, assuming there is
	matrix to be extracted.

The weighted adjacency matrix (partial correlation matrix with zeros).

#### Examples

women\_math

Data: Women and Mathematics

#### Description

A data frame containing 1190 observations (n = 1190) and 6 variables (p = 6) measured on the binary scale.

## Usage

data("women\_math")

## Format

A data frame containing 1190 observations (n = 1190) and 6 variables (p = 6) measured on the binary scale (Fowlkes et al. 1988). These data have been analyzed in Tarantola (2004) and in (Madigan and Raftery 1994). The variable descriptions were copied from (section 5.2) (section 5.2, Talhouk et al. 2012)

## Details

- 1 Lecture attendance (attend/did not attend)
- 2 Gender (male/female)
- 3 School type (urban/suburban)
- 4 "I will be needing Mathematics in my future work" (agree/disagree)
- 5 Subject preference (math/science vs. liberal arts)
- 6 Future plans (college/job)

118

#### References

Fowlkes EB, Freeny AE, Landwehr JM (1988). "Evaluating logistic models for large contingency tables." *Journal of the American Statistical Association*, **83**(403), 611–622. doi:10.1080/ 01621459.1988.10478640.

Madigan D, Raftery AE (1994). "Model selection and accounting for model uncertainty in graphical models using Occam's window." *Journal of the American Statistical Association*, **89**(428), 1535–1546.

Talhouk A, Doucet A, Murphy K (2012). "Efficient Bayesian inference for multivariate probit models with sparse inverse correlation matrices." *Journal of Computational and Graphical Statistics*, **21**(3), 739–757. doi:10.1080/10618600.2012.679239.

Tarantola C (2004). "MCMC model determination for discrete graphical models." *Statistical Modelling*, **4**(1), 39–61. doi:10.1191/1471082x04st063oa.

#### Examples

data("women\_math")

zero\_order\_cors Zero-Order Correlations

#### Description

Estimate zero-order correlations for any type of data. Note zero-order refers to the fact that no variables are controlled for (i.e., bivariate correlations). To our knowledge, this is the only Bayesian implementation in R that can estiamte Pearson's, tetrachoric (binary), polychoric (ordinal with more than two cateogries), and rank based correlation coefficients.

#### Usage

```
zero_order_cors(
    Y,
    type = "continuous",
    iter = 5000,
    mixed_type = NULL,
    progress = TRUE
)
```

#### Arguments

Y	Matrix (or data frame) of dimensions $n$ (observations) by $p$ (variables).
type	Character string. Which type of data for Y? The options include continuous, binary, ordinal, or mixed. See the note for further details.
iter	Number of iterations (posterior samples; defaults to 5000).

mixed_type	Numeric vector. An indicator of length p for which varibles should be treated as
	ranks. (1 for rank and 0 to assume normality). The default is currently to treat
	all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
progress	Logical. Should a progress bar be included (defaults to TRUE) ?

## Details

# Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option  $mixed_type$  allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise (Hoff 2007). This is accomplished by specifying an indicator vector of length p. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are treated as ranks.

#### **Dealing with Errors:**

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior\_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

#### Value

- R An array including the correlation matrices (of dimensions *p* by *p* by *iter*)
- R\_mean Posterior mean of the correlations (of dimensions *p* by *p*)

## Examples

```
iter = 250,
                progress = FALSE)
###### example 2: polychoric ####
fit <- zero_order_cors(Y+1, type = "ordinal",</pre>
                iter = 250,
                progress = FALSE)
##### example 3: rank #####
fit <- zero_order_cors(Y+1, type = "mixed",</pre>
                iter = 250,
                progress = FALSE)
## example 4: tetrachoric ##
# binary data
Y <- women_math[,1:3]</pre>
fit <- zero_order_cors(Y, type = "binary",</pre>
                iter = 250,
                progress = FALSE)
```

# Index

```
* datasets
    asd_ocd, 4
    bfi,5
    csws, 17
    depression_anxiety_t1, 19
    depression_anxiety_t2, 20
    gss, 51
    ifit, 52
    iri, 55
    ptsd, 88
    ptsd_cor1, 89
    ptsd_cor2, 90
    ptsd_cor3, 91
    ptsd_cor4,92
    rsa, 97
    Sachs, 99
    tas, 114
    women_math, 118
asd_ocd, 4
bfi.5
bggm_missing, 6
coef.estimate, 8, 107
coef.explore, 9, 107
confirm, 11, 34
constrained_posterior, 14
convergence, 16
csws, 17
depression_anxiety_t1, 19
depression_anxiety_t2, 20
estimate, 7, 22, 57, 70, 100, 108, 117
explore, 7, 11, 26, 33, 57, 71, 85, 87, 102,
         105, 117
fisher_r_to_z, 29
fisher_z_to_r, 30
formula, 11, 22, 26, 33, 40, 44
```

gen\_net, 30 gen\_ordinal, 31 ggm\_compare\_confirm, 33, 42, 48 ggm\_compare\_estimate, 23, 39, 48, 57, 72, 100, 110, 117 ggm\_compare\_explore, 42, 43, 48, 57, 73, 102, 105, 111, 117 ggm\_compare\_ppc, 23, 42, 46, 63 ggnet2, 68 ggridges, 62 gplot.layout, 68 gss, 51 ifit. 52 impute\_data, 53 iri, 55 lm, 12, 23, 27, 35, 40, 44 map, 56 mice, 7 pcor\_mat, 57 pcor\_sum, 58 pcor\_to\_cor, 60 plot.confirm, 61 plot.ggm\_compare\_ppc, 62 plot.pcor\_sum, 64 plot.predictability, 65 plot.roll\_your\_own, 66, 95 plot.select, 7, 22, 26, 67 plot.summary.estimate, 69 plot.summary.explore, 70 plot.summary.ggm\_compare\_estimate, 40, 71 plot.summary.ggm\_compare\_explore, 72 plot.summary.select.explore,73 plot.summary.var\_estimate,74 plot\_prior, 75 posterior\_predict, 76

# **INDEX**

```
posterior_samples, 77
precision, 78
predict.estimate, 79
predict.explore, 80
predict.var_estimate, 81
predictability, 23, 82
predicted_probability, 83
print.BGGM, 84
prior_belief_ggm, 85
prior_belief_var, 86
ptsd, 88
ptsd_cor1,89
ptsd_cor2, 90
ptsd_cor3, 91
ptsd_cor4,92
regression_summary, 93
roll_your_own, 94
rsa, <mark>97</mark>
Sachs, 99
select, 99
select.estimate, 22, 99, 100
select.explore, 26, 85, 87, 99, 101, 109
select.ggm_compare_estimate, 40, 99, 103
select.ggm_compare_explore, 104
select.var_estimate, 105
summary.coef, 107
summary.estimate, 107
summary.explore, 108
summary.ggm_compare_estimate, 40, 109
summary.ggm_compare_explore, 110
summary.predictability, 111
summary.select.explore, 112
summary.var_estimate, 113
tas, 114
```

var\_estimate, 114, 116

weighted\_adj\_mat, 117 women\_math, 118

zero\_order\_cors, 119